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Description	

Performance Analysis of Lossy Decode-and-Forward for Non-Orthogonal MARCs

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Abstract—Non-orthogonal transmission is considered to be one of the promising techniques for improving the throughput of the existing and future wireless communication networks. We concentrate on the transmission of both independent and correlated binary sources over a non-orthogonal multiple access relay channel (MARC), which consists of two sources, one relay, and one destination. The lossy decode-and-forward (DF), developed from the conventional DF, is adopted at the relay. Two time slots are required with non-orthogonal transmission over such network setup, while three time slots are required with the conventional orthogonal transmission. We analyze the outage probability of transmission of independent binary sources over the non-orthogonal MARC based on the theorem of multiple access channel (MAC) with a helper, which combines the Slepian-Wolf rate region and the MAC capacity region. For the performance verification, we implement a practical coding-decoding chain, which is applicable to the transmission of both independent and correlated binary sources. Exclusive-OR (XOR) based multi-user complete decoding is introduced at the relay node, and iterative joint decoding is utilized at the destination by taking into consideration the estimated intra-link error probability and correlation information between the sources. The practical simulation results are well matched with the theoretical analyses.

Index Terms—Multiple access channel with a helper, multiple access relay channels, outage probability, Slepian-Wolf theorem, Shannon’s lossy source-channel separation theorem.

I. INTRODUCTION

Cooperation among nodes in wireless cooperative networks is of great importance as it has great potential for achieving diversity gain, enhancing network throughput, and extending communication coverage even with a single antenna at each node. Several simplified cooperative network models have

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been proposed in [1]–[10]. Besides the one-way relay channel (OWRC) [1]–[3] and the two-way relay channel (TWRC) [4], [5], the multiple access relay channel (MARC) is also one common wireless cooperative network and has been thoroughly investigated in [6]–[10]. The outage probability of the MARC has been formulated under the assumption of orthogonal transmission and perfect (error-free) intra links (i.e., source-to-relay links) [6]. Lu *et al* [8] has further relaxed the assumption of error-free intra links, and re-formulated the framework for outage probability analyses. Practical joint network-channel coding (JNCC) schemes have been investigated in [9]–[11] over MARC using different channel codes, for instance, low-density parity-check (LDPC) codes [9], accumulator (ACC) aided turbo codes [10], and more generic turbo code structure [11]. However, orthogonal transmission is postulated in all the aforementioned literature.

Due to the low spectral-efficiency of the orthogonal transmission, non-orthogonal transmission has attracted a lot of attention, for instance, in coded random access techniques [12], [13]. The non-orthogonal transmissions of the uncoordinated sets of sources lead to collisions. However, the collided packets can be utilized at the destination after multi-user detection (MUD), e.g., successive interference cancellation (SIC). By allowing non-orthogonal transmissions, higher throughput can be guaranteed, which is commonly seen in machine-to-machine (M2M) communications. Similarly, the same principle can be applied to non-orthogonal transmissions of the coordinated sets of sources. The transmission of correlated sources over non-orthogonal Gaussian multiple access channel (MAC) has been investigated in [14]. The extension to the transmission of correlated sources over non-orthogonal fading MAC has been investigated in [15]. A preliminary study on the transmission of correlated sources over non-orthogonal MARC can be found in [16], where no performance verification is provided by taking into account the helper¹. In the MARC, the relay decodes the original information sequences, performs network coding (e.g., bit-wise exclusive-OR (XOR)), and forwards the network-coded sequence to the destination [7], [8]. This process at the relay is referred to as XOR based multi-user complete decoding (MUD-XOR) [17]–[19]. At the destination, joint decoding is conducted by taking into consideration the correlation information between the two sources and the side

¹Note that the paper is an extension of [16]. However, the theoretical performance analyses are not exactly the same as those conducted in [16]. We use the MAC capacity region to characterize the first MAC transmission in the paper, while in [16] we built a virtual point-to-point channel for the first MAC transmission.

information² from the relay.

The relaying protocols, e.g., amplify-and-forward (AF), compress-and-forward (CF), and decode-and-forward (DF), have been well studied in [20]–[24]. In AF, the relay just amplifies the signal sent from the source and forwards it to the destination. The drawback of AF lies in that the signal and noise are amplified simultaneously, and the noise components are accumulated, hop by hop. Thus, it does not achieve good performance, especially in the low signal-to-noise ratio (SNR) regime [23]. Due to the additional processing at the relay, CF outperforms AF in general, for instance, in OWRC [23]. In DF, the relay first decodes the received signal, and then encodes and forwards it to the destination if no errors are found in the decoded information sequence. In fact, the erroneous decoded information sequence is correlated with the original information sequence from the source, i.e., it contains useful information, which can be utilized at the destination. Even though DF has the aforementioned drawback, it has been already applied in the current LTE-A cellular system [25] due to its robustness, implementation simplicity, and applicability to existing standards.

However, for the purpose of further improving the performance and reducing latency, an enhanced version of DF called lossy DF (also called lossy forward (LF)) has been investigated in [6], [8], [10], [26], where at the relay, the received signal from the source is decoded, re-encoded, and always forwarded to the destination. Thus, error-detecting codes, e.g., cyclic redundancy check (CRC), can be removed from the relay compared to its DF counterpart, resulting in a simpler transmission mechanism at the relay. Moreover, without additional power consumption at the source, better performance in terms of outage probability can be achieved compared to DF relaying [6], [8], [10], [26].

In the paper, we apply the LF relaying to the non-orthogonal MARC, study the theoretical performance limits for the LF-MARC network, and compare the theoretical results with a series of simulation results, obtained by using practical coding and joint decoding algorithms. The main contributions of the paper are listed as follows:

- With the aim of eliminating the assumption of transmission orthogonality presented in [6]–[8], we focus on the transmissions over the non-orthogonal MARC. We analyze the outage probability for the transmission of independent binary sources over non-orthogonal MARC, where we establish a relationship among the transmit powers, geometric gains, and the distortion for the MAC composed of source-to-relay links.
- The outage probability for the transmission of independent binary sources over non-orthogonal MARC is derived by combining the non-orthogonal MAC consisting of source-to-destination links and the helper (i.e., network-coded version of the estimates of the two sources) from the relay. Due to the side information provided by the helper, the independent sources become virtually correlated at the destination. We characterize the

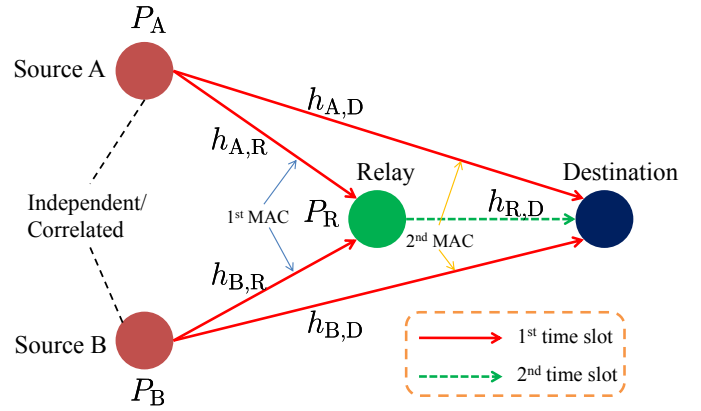


Fig. 1. The block diagram of the non-orthogonal MARC with the application of LF relaying strategy.

source coding using Slepian-Wolf theorem and channel coding using MAC capacity region. The region for lossless transmission over the non-orthogonal MAC with a helper is specified by the intersection of the Slepian-Wolf rate region and the MAC capacity region. Outage occurs if the rate pair falls outside the intersection part [27], [28]. Since the outage derivation is based on sufficient condition for the lossless transmission over the non-orthogonal MAC with a helper (through independent design of the source and channel codes), the obtained intersection region might be smaller than that derived from the sufficient and necessary conditions. Hence, the outage performance we obtain can be regarded as a theoretical upper bound. In other words, we provide a safer side network design reference.

- A practical coding-decoding structure is introduced with the applicability to the transmission of both independent and correlated binary sources over the non-orthogonal MARC. ACC aided turbo code having a simple structure is applied in the encoding process. A joint iterative decoding scheme is proposed by considering the error probability of the intra links and the correlation information between the two sources, which are estimated at the destination during each global iteration (GI), i.e., iterations among different decoders. The extrinsic log-likelihood ratio (LLR) information is exchanged among the different convolutional decoders (two for the sources, and one for the relay) and between the ACC decoders of the sources.

The remainder of this paper is organized as follows. The system model is outlined in Section II. In Section III, theoretical outage probabilities are derived, followed by the performance verification using practical coding-decoding chain in Section IV. Simulation results are presented in Section V. Finally, concluding remarks and future work are provided in Section VI.

II. SYSTEM MODEL

The non-orthogonal MARC is shown in Fig. 1, which has a symmetric topology. It consists of two sources (i.e., sources

²The term “side information” is interchangeable with the term “helper” throughout the paper.

A and B), one relay (R), and one destination (D). Each node is assumed to be equipped with a single antenna and operated in a half-duplex mode. We further assume no cooperation between the sources except for transmission timing control. The transmission round is divided into two time slots as compared to three time slots consumption in the conventional orthogonal MARC³. The binary information sequences generated from sources A and B are encoded, modulated, and simultaneously transmitted to the relay and the destination during the first time slot. The relay decodes both the source messages, performs bit-wise XOR, re-encodes, and forwards the XORed message to the destination during the second time slot.

Let the encoded and modulated symbol sequences of sources A and B be denoted by vectors \mathbf{x}_A and \mathbf{x}_B , respectively. For the sake of convenience, we assume that each symbol has unit average power, i.e., $E\{|x_A^k|^2\} = E\{|x_B^k|^2\} = 1$ for $k = 1, \dots, N$, where x_A^k and x_B^k are the k th entry of \mathbf{x}_A and \mathbf{x}_B , respectively, and N is the dimension of \mathbf{x}_A and \mathbf{x}_B . The received signal at the relay and destination during the first time-slot transmission can be expressed as

$$\mathbf{y}_{R,1} = \sqrt{P_A G_{A,R}} h_{A,R} \mathbf{x}_A + \sqrt{P_B G_{B,R}} h_{B,R} \mathbf{x}_B + \mathbf{n}_{R,1}, \quad (1)$$

$$\mathbf{y}_{D,1} = \sqrt{P_A G_{A,D}} h_{A,D} \mathbf{x}_A + \sqrt{P_B G_{B,D}} h_{B,D} \mathbf{x}_B + \mathbf{n}_{D,1}, \quad (2)$$

where all the wireless links suffer from independent and identically distributed (i.i.d.) Rayleigh block fading, distributed as $h_{A,R}, h_{B,R}, h_{A,D}, h_{B,D} \sim \mathcal{CN}(0, 1)$, P_i is the transmit power at source i , for $i \in \{A, B\}$, $G_{i,j}$ is the geometric gain between i and j , for $i \in \{A, B\}$ and $j \in \{R, D\}$. For the purpose of simplicity, we set $G_{A,D} = G_{B,D} = 1$. Each entry of additive white Gaussian noise (AWGN) vector $\mathbf{n}_{j,1}$ also follows $\mathcal{CN}(0, 1)$, for $j \in \{R, D\}$. The instantaneous individual received SNR can be written by

$$\gamma_{i,j} = G_{i,j} P_i |h_{i,j}|^2, \quad \text{for } i \in \{A, B\} \text{ and } j \in \{R, D\}, \quad (3)$$

where $|h_{i,j}|^2$ follows exponential distribution with unit mean and unit variance. In this regard, the average SNR $\bar{\gamma}_{i,j}$ is expressed as $\bar{\gamma}_{i,j} = G_{i,j} P_i$. The probability density function (pdf) of $\gamma_{i,j}$ can be expressed as

$$p(\gamma_{i,j}) = \frac{1}{P_i G_{i,j}} \exp\left(-\frac{\gamma_{i,j}}{P_i G_{i,j}}\right), \quad \text{for } i \in \{A, B\} \text{ and } j \in \{R, D\}. \quad (4)$$

Because the relay is not interested in the original information sequences sent from the sources, the relay first executes MUD and then conducts bit-wise XOR on the estimates of the information sequences transmitted from sources A and B. This process is regarded as MUD-XOR. Regardless of whether the estimates are correct or not, the relay re-encodes and modulates the XORed version of the estimates to \mathbf{x}_R , and forwards it to the destination during the second time slot⁴

³In the conventional orthogonal MARC, source A broadcasts its message to the relay and destination during the first time slot. Source B becomes active during the second time slot and behaves the same as source A. During the third time slot, the relay decodes both the source messages, performs bit-wise XOR, re-encodes, and forwards the XORed message to the destination.

⁴Due to the application of lossy DF, the relay always becomes active during the second time slot. However, with the application of DF, the relay will be silent if errors are detected after the MUD either for source A or source B.

according to LF strategy. The received signal at the destination during the second time-slot transmission is given by

$$\mathbf{y}_{D,2} = \sqrt{P_R G_{R,D}} h_{R,D} \mathbf{x}_R + \mathbf{n}_{D,2}, \quad (5)$$

where P_R denotes the transmit power at the relay, $h_{R,D}$ suffers from i.i.d. Rayleigh block fading, distributed as $h_{R,D} \sim \mathcal{CN}(0, 1)$, and each entry of $\mathbf{n}_{D,2}$ also follows $\mathcal{CN}(0, 1)$. Without loss of generality, we set $P_R = P_A = P_B = P$ throughout the paper.

III. THEORETICAL PERFORMANCE ANALYSIS

In this section, we assume that binary source A (U_A) and binary source B (U_B) are mutually independent, yielding $U_A = U_B \oplus U$ with $\Pr(U = 0) = \Pr(U = 1) = p_u = 0.5$ and \oplus denoting binary XOR operation. The theoretical performance analysis is divided into two parts, i.e., source-to-relay transmission and source-to-destination transmission with side information transmitted from the relay. We characterize the source-to-relay transmission by using the MAC capacity region, and establish a relationship among the transmit powers, geometric gains, and the distortion. We characterize the source-to-destination transmission with side information by combining the Slepian-Wolf rate region and the MAC capacity region [27], [28], which is sufficient condition for the lossless transmission of independent binary sources over the non-orthogonal MAC with a helper. Therefore, the derived outage probability can be regarded as a theoretical upper bound.

A. Source-to-Relay Transmission

Obviously, the source-to-relay channel is a two-user MAC, which we define as the first MAC in Fig. 1. The capacity region for the source-to-relay MAC is a bounded pentagonal region [27], and the whole positive orthant is divided into four non-overlapping sub-regions, shown in Fig. 2. In the figure, $\mu_{A,R} = PG_{A,R}|h_{A,R}|^2/(1 + PG_{B,R}|h_{B,R}|^2)$ and $\mu_{B,R} = PG_{B,R}|h_{B,R}|^2/(1 + PG_{A,R}|h_{A,R}|^2)$ denote the instantaneous signal-to-interference-plus-noise ratio (SINR) of source A and source B, respectively, and $C(a) = \log_2(1 + a)$ denotes the capacity function under the assumption of Gaussian codebook.

When the rate pair of sources A and B, i.e., $(R_{c,A}, R_{c,B})^5$, falls in the region \mathcal{R}_4 , both information sequences from the two sources can be recovered with arbitrarily small error probability at the relay. On the contrary, neither of the information sequences from the two sources can be successfully recovered when the rate pair falls in the region \mathcal{R}_3 . When it comes to \mathcal{R}_1 and \mathcal{R}_2 , only one of the information sequences can be perfectly recovered while the other probabilistically fails.

The probabilities that the rate pair $(R_{c,A}, R_{c,B})$ falls into regions \mathcal{R}_1 to \mathcal{R}_4 , i.e., $\Pr(\mathcal{R}_1)$ to $\Pr(\mathcal{R}_4)$, depend on the pre-determined transmission rates, instantaneous received SNRs, and instantaneous SINRs of sources A and B. They can be expressed as [29]

$$\Pr(\mathcal{R}_1) = \Pr \left[R_{c,A} > \log_2(1 + \gamma_{A,R}), R_{c,B} \leq \log_2 \left(1 + \frac{\gamma_{B,R}}{1 + \gamma_{A,R}} \right) \right], \quad (6)$$

⁵ $R_{c,A}$ and $R_{c,B}$ are the multiplications of channel coding rate and modulation order, i.e., transmission rates, for the sources A and B, respectively.

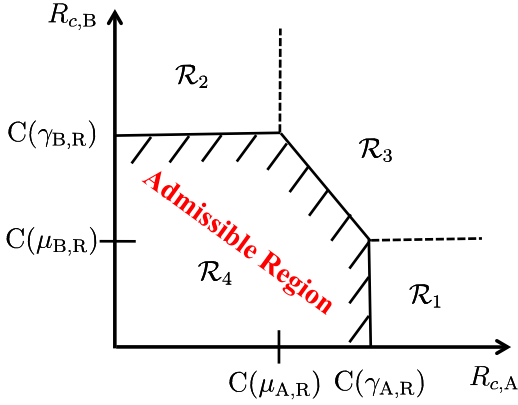


Fig. 2. Rate region for source-to-relay transmission.

$$\Pr(\mathcal{R}_2) = \Pr \left[R_{c,A} \leq \log_2 \left(1 + \frac{\gamma_{A,R}}{1 + \gamma_{B,R}} \right), R_{c,B} > \log_2(1 + \gamma_{B,R}) \right], \quad (7)$$

$$\Pr(\mathcal{R}_3) = \Pr \left[R_{c,A} > \log_2 \left(1 + \frac{\gamma_{A,R}}{1 + \gamma_{B,R}} \right), R_{c,B} > \log_2 \left(1 + \frac{\gamma_{B,R}}{1 + \gamma_{A,R}} \right), R_{c,A} + R_{c,B} > \log_2(1 + \gamma_{A,R} + \gamma_{B,R}) \right], \quad (8)$$

$$\Pr(\mathcal{R}_4) = \Pr \left[R_{c,A} < \log_2 \left(1 + \frac{\gamma_{A,R}}{1 + \gamma_{B,R}} \right), R_{c,B} < \log_2(1 + \gamma_{B,R}) \right] + \Pr \left[\log_2 \left(1 + \frac{\gamma_{A,R}}{1 + \gamma_{B,R}} \right) \leq R_{c,A} < \log_2(1 + \gamma_{A,R}), R_{c,A} + R_{c,B} < \log_2(1 + \gamma_{A,R} + \gamma_{B,R}) \right]. \quad (9)$$

When evaluating \mathcal{R}_1 and \mathcal{R}_2 , after canceling the successfully decoded information sequence, the calculation of the distortion of the other information sequence becomes the same as that in a point-to-point (P2P) transmission problem. Therefore, the distortion can be obtained by using the Shannon's lossy source-channel separation theorem [6], [10]. For instance, when the rate pair falls into \mathcal{R}_1 , we have $\hat{U}_A \neq U_A$, $\hat{U}_B = U_B$ (For the other sub-regions, more details can be found in Table I) with \hat{U}_A, \hat{U}_B being the estimates of U_A, U_B at the relay. The distortion of U_A , denoted by D , is determined by⁶

$$R(D)R_{c,A} \leq C(\gamma_{A,R}), \quad (10)$$

where $R(D)$ represents the binary rate distortion function. Setting $\Phi(\gamma_{A,R}) = C(\gamma_{A,R})/R_{c,A}$, the calculation of the minimum

⁶More strictly, we should use the binary constellation constrained capacity (CCC) here. However, if the instantaneous SNR is low, the Gaussian capacity is almost equal to CCC [30]. If the instantaneous SNR is large, the distortion would be zero as long as the fixed transmission rate is less than the CCC. Hence, the use of the binary rate distortion function and the Gaussian capacity is reasonable when using the lossy source-channel separation theorem [1].

TABLE I
RELATIONSHIP BETWEEN THE SUB-REGIONS AND THE DECODING OUTCOMES AT THE RELAY.

\mathcal{R}_1	$\hat{U}_A \neq U_A, \hat{U}_B = U_B$
\mathcal{R}_2	$\hat{U}_A = U_A, \hat{U}_B \neq U_B$
\mathcal{R}_3	$\hat{U}_A \neq U_A, \hat{U}_B \neq U_B$
\mathcal{R}_4	$\hat{U}_A = U_A, \hat{U}_B = U_B$

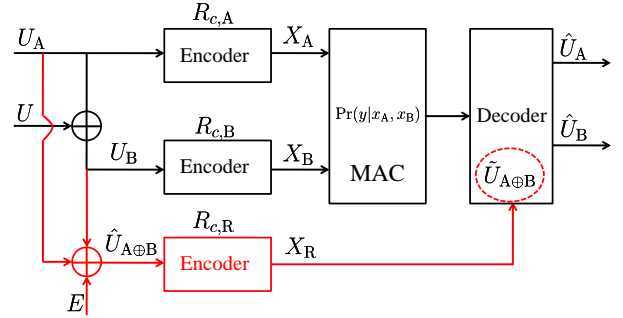


Fig. 3. Illustration of MAC with a helper.

distortion of U_A , denoted by D_{\min} , can be further computed by [8]

$$D_{\min} = \begin{cases} H_b^{-1}[1 - \Phi(\gamma_{A,R})], & \text{for } \Phi^{-1}(0) \leq \gamma_{A,R} \leq \Phi^{-1}(1), \\ 0, & \text{for } \gamma_{A,R} \geq \Phi^{-1}(1), \end{cases} \quad (11)$$

where $H_b(p) = -p \log_2(p) - (1-p) \log_2(1-p)$ denotes the binary entropy function, $H_b^{-1}(\cdot)$ denotes its inverse function, and $\Phi^{-1}(a) = 2^{aR_{c,A}} - 1$ is the inverse function of $\Phi(\cdot)$. The approximated closed-form expression of $H_b^{-1}(\cdot)$ is given in [1]. The relationship between the XORed version of the estimates $\hat{U}_{A\oplus B} = \hat{U}_A \oplus \hat{U}_B$ and its original one (denoted by $U_{A\oplus B} = U_A \oplus U_B$) can also be modeled by bit-flipping model with bit-flipping probability p_e ,

$$\hat{U}_{A\oplus B} = U_{A\oplus B} \oplus E, \quad (12)$$

where $\Pr(E=1) = p_e$. Equation (12) can be further expressed as $\hat{U}_A = U_A \oplus E$. In this sense, we set $p_e = D_{\min}$. We can calculate the distortion for U_B when the rate pair falls into \mathcal{R}_2 in the same manner.

We ignore \mathcal{R}_3 in the calculation of outage probability for the following two reasons: 1) If both sources are erroneous, the helper cannot improve the performance of the second MAC (see Fig. 1) consisting of source-to-destination links. 2) When the SNR increases, the probability of $(R_{c,A}, R_{c,B})$ falling in \mathcal{R}_3 becomes very small. Therefore, the ratio of $\Pr\{\mathcal{R}_3\}/\sum_{i=1, i \neq 3}^4 \Pr\{\mathcal{R}_i\}$ approaches zero in the high SNR regime.

B. MAC with a Helper

In the non-orthogonal MARC, the source-to-destination transmission during the first time slot combined with the relay-to-destination transmission during the second time slot can be regarded as MAC with a helper, as shown in Fig. 3.

where

$$\begin{aligned}
C_1 &= \{p_e = 0 \wedge p_d = 0\}, \\
C_2 &= \{p_e = 0 \wedge p_d \neq 0\}, \\
C_3 &= \{p_e \neq 0 \wedge p_d = 0\}, \\
C_4 &= \{p_e \neq 0 \wedge p_d \neq 0\}.
\end{aligned} \tag{27}$$

All the above four events will be transferred into different intervals of a three-dimensional vector consisting of $\gamma_{A,R}$, $\gamma_{B,R}$, $\gamma_{R,D}$. In addition to the effect of direct links from the sources to the destination, i.e., $\gamma_{A,D}$ and $\gamma_{B,D}$, the probability of successful transmission $\Pr\{\mathcal{S}\}$ can be calculated by five-fold integrals, i.e.,

$$\Pr\{\mathcal{S}|C_i\}\Pr\{C_i\} = \int_{\mathbb{V}_i} \cdots \int p(\gamma_{A,R})p(\gamma_{B,R})p(\gamma_{R,D})p(\gamma_{A,D})p(\gamma_{B,D}) d\gamma_{A,R}d\gamma_{B,R}d\gamma_{R,D}d\gamma_{A,D}d\gamma_{B,D}, \quad i \in \{1, 2, 3, 4\}. \tag{28}$$

where \mathbb{V}_1 to \mathbb{V}_4 are defined in (29)–(32) with \vee denotes logical “or”. More details on (28) are provided in Appendix B.

IV. PRACTICAL CODING AND JOINT DECODING

In this section, we describe a structure that implements a practical coding-decoding chain for transmission of both independent and correlated sources over the non-orthogonal MARC. Let us assume $0 < \Pr(U = 1) = p_u \leq 0.5$. The difference from the theoretical performance analyses is that we also include the case of transmitting correlated sources over the non-orthogonal MARC in the practical simulations. Notions used in this section are defined as follows.

- $L_i(x_A^k)$: initial channel LLR for x_A^k ;
- $L_i(x_B^k)$: initial channel LLR for x_B^k ;
- $L_a(x_A^k)$: *a priori* LLR for x_A^k during the GI;
- $L_a(x_B^k)$: *a priori* LLR for x_B^k during the GI;
- $L_a(u_A^k)$: *a priori* LLR for the k th entry of \mathbf{u}_A (a sequence of realizations of U_A), i.e., u_A^k , during the GI;
- $L_a(u_B^k)$: *a priori* LLR for the k th entry of \mathbf{u}_B (a sequence of realizations of U_B), i.e., u_B^k , during the GI;
- $L_a(u_R^k)$: *a priori* LLR for the k th entry of \mathbf{u}_R (a sequence of realizations of $\hat{U}_{A \oplus B}$), i.e., u_R^k , during the GI;
- $L_e(x_A^k)$: extrinsic LLR for x_A^k during the GI;
- $L_e(x_B^k)$: extrinsic LLR for x_B^k during the GI;
- $L_e(u_A^k)$: extrinsic LLR for u_A^k during the GI;
- $L_e(u_B^k)$: extrinsic LLR for u_B^k during the GI;
- $L_e(u_R^k)$: extrinsic LLR for u_R^k during the GI;
- $L_p(u_A^k)$: *a posteriori* LLR for u_A^k ;
- $L_p(u_B^k)$: *a posteriori* LLR for u_B^k ;
- $L_p(u_R^k)$: *a posteriori* LLR for u_R^k ;
- K : the length of the binary information sequences;
- \hat{p}_u : the estimate of correlation coefficient p_u ;
- \hat{p}_e : the estimate of the bit-flipping probability p_e ;
- $y_{R,1}^k$: the k th entry of $\mathbf{y}_{R,1}$;
- $y_{D,1}^k$: the k th entry of $\mathbf{y}_{D,1}$.

A. Channel Coding

We use the identical structure⁸ of channel code for the sources and the relay, which is shown in Fig. 5. The structure is known as ACC aided turbo code, which has been widely applied in cooperative communication systems [6], [8], [10]. It consists of three components, i.e., rate- R_c convolutional code (CC), interleaver (e.g., Π_A), and rate-1 ACC. The overall channel code rate is equal to R_c . The modulation scheme we consider here is binary phase shift keying (BPSK) with $0 \rightarrow 1$ and $1 \rightarrow -1$.

Compared to the more advanced LDPC codes, the ACC aided turbo codes can have a simpler structure and subsequently lower implementation complexity. Nevertheless, it has been demonstrated in [31] that the ACC aided turbo code with the generator polynomial of the non-recursive non-systematic convolutional code (NSNRCC) being $G = ([3, 2])_8$ approaches the Shannon limit within 1.2 dB over AWGN channels at the BER level of 10^{-4} . The performance loss, compared to the more advanced LDPC codes, is compensated for by the low computational complexity and power consumption. Hence, we consider the ACC aided turbo code with the generator polynomial of the NSNRCC being $G = ([3, 2])_8$ in the practical simulations due to its satisfactory performance-complexity trade-off.

B. MUD-XOR at Relay

The frame structure of the MUD-XOR at relay is depicted in Fig. 6, where the ACC decoder is denoted by ACC^{-1} , the de-interleavers are denoted by Π_A^{-1} , and Π_B^{-1} , the convolutional decoder is denoted by CC^{-1} , and the demapper is denoted by DMAP at the relay. Decoder input and output are marked with different colors for the purpose of better illustration. After receiving the signals from sources A and B, the relay uses the demapping rule [32] to calculate the initial LLRs from the channels, which are the inputs for the two turbo decoders associated with the two sources. The detailed demapping rule is shown as follows:

$$L_i(x_A^k) = \ln \left(\frac{\sum_{i=\pm 1} \Pr(x_A^k = 1, x_B^k = i | y_{R,1}^k)}{\sum_{i=\pm 1} \Pr(x_A^k = -1, x_B^k = i | y_{R,1}^k)} \right), \tag{33}$$

$$L_i(x_B^k) = \ln \left(\frac{\sum_{i=\pm 1} \Pr(x_B^k = 1, x_A^k = i | y_{R,1}^k)}{\sum_{i=\pm 1} \Pr(x_B^k = -1, x_A^k = i | y_{R,1}^k)} \right). \tag{34}$$

Both local iteration (LI) and GI are involved in the MUD-XOR process, as shown in Fig. 6. For the LI, i.e., iterations between the constituent decoders (convolutional decoder and ACC decoder), we use the Bahl-Cocke-Jelinek-Raviv (BCJR) decoding algorithm [33]. During the GI⁹, the information exchange is expressed by (35)–(38).

⁸The same structure does not necessarily mean the same code. Here, we use the same CC and ACC but different random interleavers.

⁹For the purpose of simplicity, we omit the iteration indexes in all the following equations.

$$\begin{aligned} \mathbb{V}_1 = & \underbrace{\{\gamma_{A,R} \geq \Phi^{-1}(1)(1 + \gamma_{B,R}) \wedge \gamma_{B,R} \geq \Phi^{-1}(1)\} \vee \{\Phi^{-1}(1) \leq \gamma_{A,R} \leq \Phi^{-1}(1)(1 + \gamma_{B,R}) \wedge \gamma_{A,R} + \gamma_{B,R} \geq 2^{R_{c,A} + R_{c,B}} - 1\}}_{\{p_e=0 | \mathcal{R}_d\}} \\ & \wedge \underbrace{\{\gamma_{R,D} \geq \Phi^{-1}(1)\}}_{\{p_d=0\}} \wedge \underbrace{\{\gamma_{A,D} \geq \Phi^{-1}(0) \wedge \gamma_{B,D} \geq \Phi^{-1}(0) \wedge \gamma_{A,D} + \gamma_{B,D} \geq \Phi^{-1}(1)\}}_{\{S | p_e=0, p_d=0\}}, \end{aligned} \quad (29)$$

$$\begin{aligned} \mathbb{V}_2 = & \underbrace{\{\gamma_{A,R} \geq \Phi^{-1}(1)(1 + \gamma_{B,R}) \wedge \gamma_{B,R} \geq \Phi^{-1}(1)\} \vee \{\Phi^{-1}(1) \leq \gamma_{A,R} \leq \Phi^{-1}(1)(1 + \gamma_{B,R}) \wedge \gamma_{A,R} + \gamma_{B,R} \geq 2^{R_{c,A} + R_{c,B}} - 1\}}_{\{p_e=0 | \mathcal{R}_d\}} \\ & \wedge \underbrace{\{\Phi^{-1}(0) \leq \gamma_{R,D} \leq \Phi^{-1}(1)\}}_{\{p_d \neq 0\}} \wedge \underbrace{\{\gamma_{A,D} \geq \Phi^{-1}[H_b(p_d)] \wedge \gamma_{B,D} \geq \Phi^{-1}[H_b(p_d)] \wedge \gamma_{A,D} + \gamma_{B,D} \geq \Phi^{-1}[1 + H_b(p_d)]\}}_{\{S | p_e=0, p_d \neq 0\}}, \end{aligned} \quad (30)$$

$$\begin{aligned} \mathbb{V}_3 = & \underbrace{\{\gamma_{A,R} < \Phi^{-1}(1) \wedge \gamma_{B,R} > \Phi^{-1}(1)(1 + \gamma_{A,R})\}}_{\{p_e \neq 0 | \mathcal{R}_1\}} \vee \underbrace{\{\gamma_{B,R} < \Phi^{-1}(1) \wedge \gamma_{A,R} > \Phi^{-1}(1)(1 + \gamma_{B,R})\}}_{\{p_e \neq 0 | \mathcal{R}_2\}} \\ & \wedge \underbrace{\{\gamma_{R,D} \geq \Phi^{-1}(1)\}}_{\{p_d=0\}} \wedge \underbrace{\{\gamma_{A,D} \geq \Phi^{-1}[H_b(p_e)] \wedge \gamma_{B,D} \geq \Phi^{-1}[H_b(p_e)] \wedge \gamma_{A,D} + \gamma_{B,D} \geq \Phi^{-1}[1 + H_b(p_e)]\}}_{\{S | p_e \neq 0, p_d=0\}}, \end{aligned} \quad (31)$$

$$\begin{aligned} \mathbb{V}_4 = & \underbrace{\{\gamma_{A,R} < \Phi^{-1}(1) \wedge \gamma_{B,R} > \Phi^{-1}(1)(1 + \gamma_{A,R})\}}_{\{p_e \neq 0 | \mathcal{R}_1\}} \vee \underbrace{\{\gamma_{B,R} < \Phi^{-1}(1) \wedge \gamma_{A,R} > \Phi^{-1}(1)(1 + \gamma_{B,R})\}}_{\{p_e \neq 0 | \mathcal{R}_2\}} \\ & \wedge \underbrace{\{\Phi^{-1}(0) \leq \gamma_{R,D} \leq \Phi^{-1}(1)\}}_{\{p_d \neq 0\}} \wedge \underbrace{\{\gamma_{A,D} \geq \Phi^{-1}[H_b(p_e * p_d)] \wedge \gamma_{B,D} \geq \Phi^{-1}[H_b(p_e * p_d)] \wedge \gamma_{A,D} + \gamma_{B,D} \geq \Phi^{-1}[1 + H_b(p_e * p_d)]\}}_{\{S | p_e \neq 0, p_d \neq 0\}}. \end{aligned} \quad (32)$$

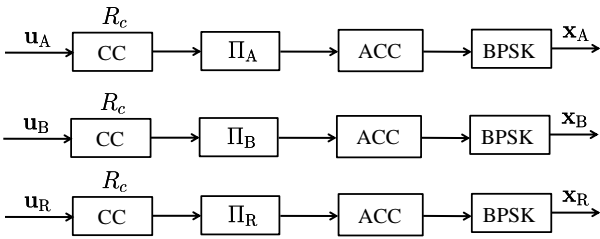


Fig. 5. Channel coding and modulation structure at the two sources and the relay.

1) *Information Exchange between the CC⁻¹s*: The information exchange between the two convolutional decoders follows the LLR updating rule in [34], characterized by the $f_c(\cdot, \cdot)$ function, which is defined in (35) and (36).

2) *Information Exchange between the ACC⁻¹s of Sources A and B*: It should be noted that (37) and (38) follow the modified demapping rule, which takes the extrinsic information from the other ACC decoder into consideration. As shown in these formulations, (37) and (38) are functions of $y_{R,1}^k$, P , $G_{A,R}$, $G_{B,R}$, $h_{A,R}$, $h_{B,R}$, and extrinsic LLRs from the ACC decoders. More details on (37) can be found in Appendix C.

In practice, the exact knowledge about p_u is not available at the relay. However, it can be estimated and calculated during

each GI as [34],

$$\hat{p}_u = \frac{1}{K} \sum_{k=1}^K \frac{\exp\{L_p(u_A^k)\} + \exp\{L_p(u_B^k)\}}{(1 + \exp\{L_p(u_A^k)\})(1 + \exp\{L_p(u_B^k)\})}. \quad (39)$$

After reaching the stop criterion or achieving the maximum number of iterations, the relay performs bit-wise XOR on the estimates of sources A and B (i.e., $\hat{\mathbf{u}}_A$ and $\hat{\mathbf{u}}_B$ in Fig. 6), re-encodes, modulates, and then transmits it to the destination regardless of whether errors are contained in the estimates or not.

C. Joint Decoding at Destination

The frame structure of the joint decoding is shown in Fig. 7, where global and local iterations are also needed during the decoding procedures. Similar to Fig. 6, decoder input and output are also marked with different colors. In this subsection, we reuse all the notations, which appear in the last subsection.

The GI also consists of two major parts, i.e., information exchange among the CC⁻¹s and information exchange between the ACC⁻¹s of sources A and B.

1) *Information Exchange among the CC⁻¹s*: Different from the boxplus operations in [6], the information exchange here takes into consideration of the probability of the intra-link errors. The *a priori* LLR information of source A, output of the modified boxplus operation in Fig. 7, can be expressed as

$$L_a(u_A^k) = \ln \left(\frac{\Pr(\oplus\{u_B^k, u_R^k, e^k\} = 0)}{\Pr(\oplus\{u_B^k, u_R^k, e^k\} = 1)} \right), \quad (40)$$

$$L_a(u_A^k) = f_c(L_e(u_B^k), \hat{p}_u) = \ln \left(\frac{(1 - \hat{p}_u) \exp\{L_e(u_B^k)\} + \hat{p}_u}{(1 - \hat{p}_u) + \hat{p}_u \exp\{L_e(u_B^k)\}} \right), \quad (35)$$

$$L_a(u_B^k) = f_c(L_e(u_A^k), \hat{p}_u) = \ln \left(\frac{(1 - \hat{p}_u) \exp\{L_e(u_A^k)\} + \hat{p}_u}{(1 - \hat{p}_u) + \hat{p}_u \exp\{L_e(u_A^k)\}} \right). \quad (36)$$

$$L_a(x_A^k) = \ln \left(\frac{\exp(L_e(x_B^k) - |y_{R,1}^k - \sqrt{PG_{A,R}}h_{A,R} - \sqrt{PG_{B,R}}h_{B,R}|^2) + \exp(-|y_{R,1}^k - \sqrt{PG_{A,R}}h_{A,R} + \sqrt{PG_{B,R}}h_{B,R}|^2)}{\exp(-|y_{R,1}^k + \sqrt{PG_{A,R}}h_{A,R} + \sqrt{PG_{B,R}}h_{B,R}|^2) + \exp(L_e(x_B^k) - |y_{R,1}^k + \sqrt{PG_{A,R}}h_{A,R} - \sqrt{PG_{B,R}}h_{B,R}|^2)} \right), \quad (37)$$

$$L_a(x_B^k) = \ln \left(\frac{\exp(L_e(x_A^k) - |y_{R,1}^k - \sqrt{PG_{A,R}}h_{A,R} - \sqrt{PG_{B,R}}h_{B,R}|^2) + \exp(-|y_{R,1}^k + \sqrt{PG_{A,R}}h_{A,R} - \sqrt{PG_{B,R}}h_{B,R}|^2)}{\exp(-|y_{R,1}^k + \sqrt{PG_{A,R}}h_{A,R} + \sqrt{PG_{B,R}}h_{B,R}|^2) + \exp(L_e(x_A^k) - |y_{R,1}^k - \sqrt{PG_{A,R}}h_{A,R} + \sqrt{PG_{B,R}}h_{B,R}|^2)} \right), \quad (38)$$

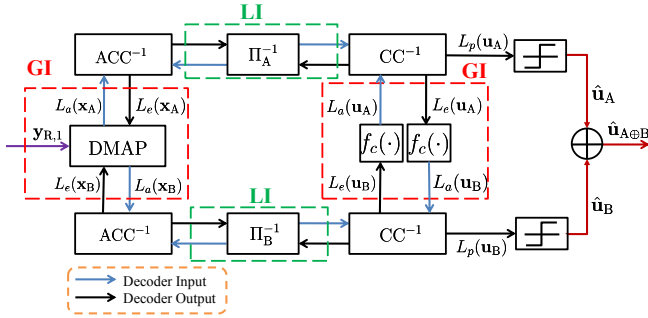


Fig. 6. Frame structure of MUD-XOR at the relay.

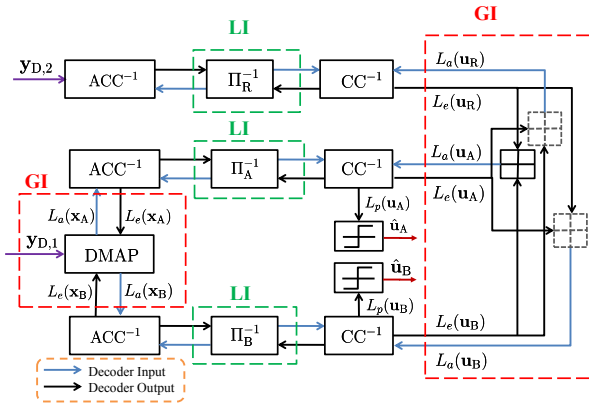


Fig. 7. Frame structure of joint decoding at the destination.

where \oplus is implemented in the bit-wise mode, and e^k is the k th entry of \mathbf{e} (a sequence of realizations of E). Similarly, the *a priori* LLR information of source B and the relay can be expressed as

$$L_a(u_B^k) = \ln \left(\frac{\Pr(\oplus\{u_A^k, u_R^k, e^k\} = 0)}{\Pr(\oplus\{u_A^k, u_R^k, e^k\} = 1)} \right), \quad (41)$$

$$L_a(u_R^k) = \ln \left(\frac{\Pr(\oplus\{u_A^k, u_B^k, e^k\} = 0)}{\Pr(\oplus\{u_A^k, u_B^k, e^k\} = 1)} \right). \quad (42)$$

There exist $2^3 = 8$ combinations for $\{u_B^k, u_R^k, e^k\}$ in (40),

i.e., $\{u_B^k = 0, u_R^k = 0, e^k = 0\}$, $\{u_B^k = 0, u_R^k = 0, e^k = 1\}$, $\{u_B^k = 0, u_R^k = 1, e^k = 0\}$, $\{u_B^k = 0, u_R^k = 1, e^k = 1\}$, $\{u_B^k = 1, u_R^k = 0, e^k = 0\}$, $\{u_B^k = 1, u_R^k = 0, e^k = 1\}$, $\{u_B^k = 1, u_R^k = 1, e^k = 0\}$, and $\{u_B^k = 1, u_R^k = 1, e^k = 1\}$. Four of the combinations are included in the numerator of (40) while the remaining are included in the denominator of (40). After some manipulations, (40)–(42) can be further expressed in (43)–(45). We offer detailed information on (43) in Appendix C. Similarly, (44) and (45) can be derived in the same manner as (43).

Similarly to (39), the bit-flipping probability p_e at the first MAC can be estimated at the destination by (46). More details on (46) are also provided in Appendix C.

2) *Information Exchange between the ACC⁻¹s of Sources A and B*: Similar to (37) and (38) in the MUD-XOR process, the information updating rule for $L_a(x_A^k)$ and $L_a(x_B^k)$ is expressed in (47) and (48). As shown in these formulations, (47) and (48) are functions of $\mathbf{y}_{D,1}^k$, P , $G_{A,D}$, $G_{B,D}$, $h_{A,D}$, $h_{B,D}$, and extrinsic LLRs from the ACC decoders.

V. SIMULATION RESULTS

In this section, we draw the theoretical and practical simulation results in terms of the outage probability and FER over the non-orthogonal MARC. All the transmission rates are set to be 0.5. The correlation coefficient between the sources ranges from 0 to 0.5. In the practical coding-decoding chain, we set $K = 1000$ (i.e., $N = 2000$) and use random interleavers [35]. The GI is performed after every LI, and the maximum number of GI is set to 15. Orthogonal transmission with imperfect intra links from [8] is considered as a benchmark scheme. Four different scenarios are taken into consideration.

1) *Scenario One (Equal Distance for All the Links)*: In this scenario, we assume $d_{R,D} = d_{A,R} = d_{B,R} = d_{A,D} = d_{B,D}$ with $d_{R,D}$, $d_{A,R}$, $d_{B,R}$, $d_{A,D}$, $d_{B,D}$ denoting the distances of relay-to-destination, source A-to-relay, source B-to-relay, source A-to-destination, and source B-to-destination, respectively. In other words, the geometric gains have the following relationship: $G_{R,D} = G_{A,R} = G_{B,R} = G_{A,D} = G_{B,D}$, by ignoring shadowing variations.

2) *Scenario Two (Relay in the Middle)*: In this scenario¹⁰, we assume $d_{R,D} = d_{A,R} = d_{B,R} = 0.6 \times d_{A,D} = 0.6 \times d_{B,D}$. In

¹⁰In the middle means the relay has the same distance to the two sources and the destination.

$$L_a(u_A^k) = \ln \left(\frac{(1 - \hat{p}_e)(1 - \hat{p}_u) \exp\{L_e(u_B^k) + L_e(u_R^k)\} + (1 - \hat{p}_e)\hat{p}_u + \hat{p}_e(1 - \hat{p}_u) \exp\{L_e(u_B^k)\} + \hat{p}_e\hat{p}_u \exp\{L_e(u_R^k)\}}{(1 - \hat{p}_e)\hat{p}_u \exp\{L_e(u_B^k)\} + (1 - \hat{p}_e)(1 - \hat{p}_u) \exp\{L_e(u_R^k)\} + \hat{p}_e\hat{p}_u \exp\{L_e(u_B^k) + L_e(u_R^k)\} + \hat{p}_e(1 - \hat{p}_u)} \right), \quad (43)$$

$$L_a(u_B^k) = \ln \left(\frac{(1 - \hat{p}_e)(1 - \hat{p}_u) \exp\{L_e(u_A^k) + L_e(u_R^k)\} + (1 - \hat{p}_e)\hat{p}_u + \hat{p}_e(1 - \hat{p}_u) \exp\{L_e(u_A^k)\} + \hat{p}_e\hat{p}_u \exp\{L_e(u_R^k)\}}{(1 - \hat{p}_e)\hat{p}_u \exp\{L_e(u_A^k)\} + (1 - \hat{p}_e)(1 - \hat{p}_u) \exp\{L_e(u_R^k)\} + \hat{p}_e\hat{p}_u \exp\{L_e(u_A^k) + L_e(u_R^k)\} + \hat{p}_e(1 - \hat{p}_u)} \right), \quad (44)$$

$$L_a(u_R^k) = \ln \left(\frac{(1 - \hat{p}_e)(1 - \hat{p}_u)(1 + \exp\{L_e(u_A^k) + L_e(u_B^k)\}) + \hat{p}_e\hat{p}_u(\exp\{L_e(u_A^k)\} + \exp\{L_e(u_B^k)\})}{(1 - \hat{p}_e)\hat{p}_u(\exp\{L_e(u_A^k)\} + \exp\{L_e(u_B^k)\}) + \hat{p}_e(1 - \hat{p}_u)(1 + \exp\{L_e(u_A^k) + L_e(u_B^k)\})} \right). \quad (45)$$

$$\hat{p}_e = \frac{1}{K} \sum_{k=1}^K \frac{\exp\{L_p(u_A^k) + L_p(u_B^k)\} + \exp\{L_p(u_A^k) + L_p(u_R^k)\} + \exp\{L_p(u_B^k) + L_p(u_R^k)\} + 1}{(1 + \exp\{L_p(u_A^k)\})(1 + \exp\{L_p(u_B^k)\})(1 + \exp\{L_p(u_R^k)\})}. \quad (46)$$

$$L_a(x_A^k) = \ln \left(\frac{\exp(L_e(x_B^k)) \exp(-|y_{D,1}^k - \sqrt{PG_{A,D}}h_{A,D} - \sqrt{PG_{B,D}}h_{B,D}|^2) + \exp(-|y_{D,1}^k - \sqrt{PG_{A,D}}h_{A,D} + \sqrt{PG_{B,D}}h_{B,D}|^2)}{\exp(-|y_{D,1}^k + \sqrt{PG_{A,D}}h_{A,D} + \sqrt{PG_{B,D}}h_{B,D}|^2) + \exp(L_e(x_B^k)) \exp(-|y_{D,1}^k + \sqrt{PG_{A,D}}h_{A,D} - \sqrt{PG_{B,D}}h_{B,D}|^2)} \right), \quad (47)$$

$$L_a(x_B^k) = \ln \left(\frac{\exp(L_e(x_A^k)) \exp(-|y_{D,1}^k - \sqrt{PG_{A,D}}h_{A,D} - \sqrt{PG_{B,D}}h_{B,D}|^2) + \exp(-|y_{D,1}^k + \sqrt{PG_{A,D}}h_{A,D} - \sqrt{PG_{B,D}}h_{B,D}|^2)}{\exp(-|y_{D,1}^k + \sqrt{PG_{A,D}}h_{A,D} + \sqrt{PG_{B,D}}h_{B,D}|^2) + \exp(L_e(x_A^k)) \exp(-|y_{D,1}^k - \sqrt{PG_{A,D}}h_{A,D} + \sqrt{PG_{B,D}}h_{B,D}|^2)} \right). \quad (48)$$

other words, the geometric gains have the following relationship: $G_{R,D} = G_{A,R} = G_{B,R} = G_{A,D} + 7.81$ dB = $G_{B,D} + 7.81$ dB under the condition that the path-loss exponent is set to 3.52 [36].

3) *Scenario Three (Relay Closer to the Sources)*: In this scenario, we assume $d_{A,R} = d_{B,R} = 0.4 \times d_{A,D} = 0.4 \times d_{B,D}$ and $d_{R,D} = 0.8 \times d_{A,D} = 0.8 \times d_{B,D}$. In other words, the geometric gains have the following relationship: $G_{A,R} = G_{B,R} = G_{A,D} + 14.01$ dB = $G_{B,D} + 14.01$ dB and $G_{R,D} = G_{A,D} + 3.40$ dB = $G_{B,D} + 3.40$ dB.

4) *Scenario Four (Relay Closer to the Destination)*: In this scenario, we assume $d_{A,R} = d_{B,R} = 0.8 \times d_{A,D} = 0.8 \times d_{B,D}$ and $d_{R,D} = 0.4 \times d_{A,D} = 0.4 \times d_{B,D}$. In other words, the geometric gains have the following relationship: $G_{A,R} = G_{B,R} = G_{A,D} + 3.40$ dB = $G_{B,D} + 3.40$ dB and $G_{R,D} = G_{A,D} + 14.01$ dB = $G_{B,D} + 14.01$ dB.

A. Independent Sources

The simulation results for the case of independent sources are provided in Fig. 8, where ‘‘FER’’ represents the FER curves obtained by using the practical coding-decoding chain described in Section IV, ‘‘Theo’’ represents the theoretical results of the outage probability for the non-orthogonal MARC given by (25), and ‘‘Theo [8]’’ represents the theoretical results of the outage probability for the orthogonal MARC from [8] with imperfect intra links. Compared to the case in [8], the performance loss is very limited for the non-orthogonal MARC also with imperfect intra links. Second order diversity can be achieved for all the scenarios. The gap between theoretical outage probability and FER obtained by using ACC aided turbo code is within 4 dB for all the scenarios at the FER level of 10^{-3} . It is not difficult to observe that *scenario*

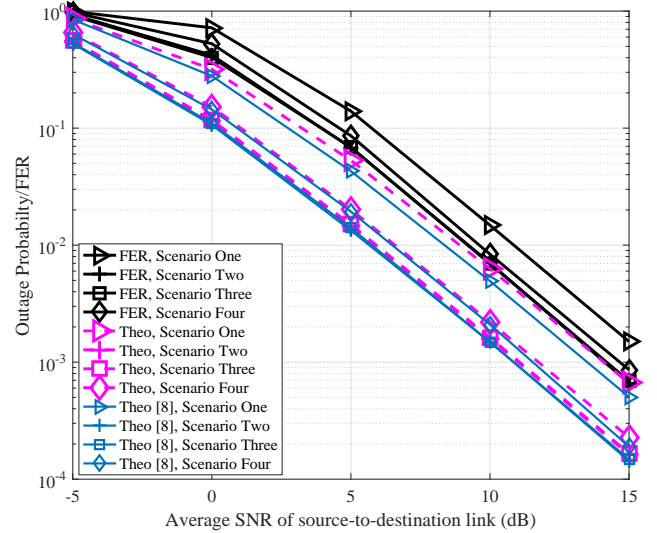


Fig. 8. Outage probabilities and FERs of transmitting independent sources over the non-orthogonal MARC.

one is the worst among all the four scenarios while *scenario two* and *scenario three* are the best and have almost the same performance in terms of both FER and theoretical outage probability. In this sense, the best relay position should be closer to the sources or in the middle between the sources and destination.

The throughput of the non-orthogonal MARC is shown in Fig. 9, where the overall time slots are taken into consideration. The results from [8] are also offered as benchmark schemes. From the simulation curves, we could easily observe that non-orthogonal transmission significantly outperforms its

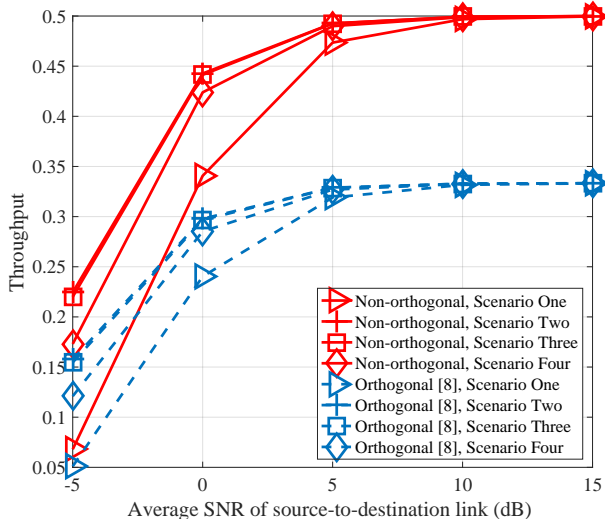


Fig. 9. Throughput of transmitting independent sources over the non-orthogonal MARC.

orthogonal counterpart. At the high SNR regime, the throughput of the non-orthogonal MARC is roughly 1.5 times of that of the orthogonal MARC.

B. Correlated Sources

In the theoretical outage analyses for the case of correlated sources, obtaining distortion for the first MAC is an open problem [27]. Hence, we evaluate the performance of such case by simulations only. We perform the simulations via a practical coding-decoding structure as the one used in the case of independent sources. This could offer performance tendency intuitively of transmitting correlated sources over the non-orthogonal MARC. The simulation results are shown in Fig. 10. We omit the curve for *scenario three*, since it is almost the same as that for *scenario two*¹¹. The performance improves as the correlation between the two sources increases. It should be noticed that second order diversity can be achieved for all the scenarios. When p_u approaches zero, all the scenarios have almost the same outage performance, since the relay becomes helpless and the transmission only relies on the direct links.

VI. CONCLUSIONS AND FUTURE WORK

We have calculated the outage probability for the transmission of independent sources over the non-orthogonal fading MARC, which is based on the sufficient condition of lossless communication over MAC with the aid of a helper. Since we use sufficient condition only, the derived outage is a theoretical upper bound. Thus, the outage derivation provides a safer side network design reference. It has been found that the throughput of the non-orthogonal MARC can be significantly improved compared to its orthogonal counterpart.

¹¹Performance similarity between the curves for *scenario two* and *scenario three* is also observed in Fig. 8.

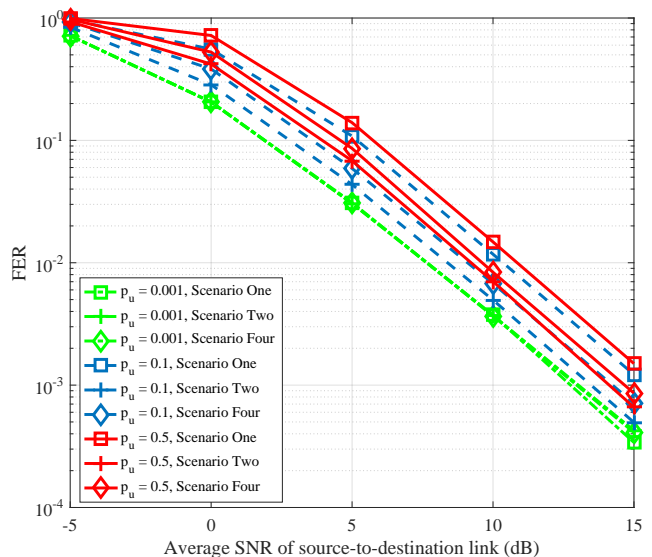


Fig. 10. FERs of transmitting correlated sources over the non-orthogonal MARC.

A computationally-/energy-efficient scheme with ACC-aided turbo code has been then proposed, where the FER performance has been shown to closely approach the theoretical upper bound of the outage probability.

Time and power allocation are potential tools for the improvement of the outage performance, which will be considered as our future work. The theoretical outage analysis we have provided is only for the case of independent sources, and the correlated case is left as future study. The necessary and sufficient conditions for the MAC with a helper are also a potential problem for future investigation.

The sources keep silent during the second time slot in the paper. A natural extension would be that additional parity bits are transmitted from the sources during the second time slot. Therefore, a comprehensive study is needed to identify its potential benefits over the transmission scheme studied in the paper. The optimization of encoding-decoding chain and the selection of better codes are also left for future investigation.

APPENDIX A DERIVATION OF (16) – (18)

According to the chain rule for entropy, the joint entropy of U_A , U_B , $\hat{U}_{A\oplus B}$, and $\tilde{U}_{A\oplus B}$ can be written by

$$H(U_A, U_B, \hat{U}_{A\oplus B}, \tilde{U}_{A\oplus B}) = H(U_A) + H(U_B|U_A) + H(\hat{U}_{A\oplus B}|U_A, U_B) + H(\tilde{U}_{A\oplus B}|U_A, U_B, \hat{U}_{A\oplus B}), \quad (49)$$

where $H(U_A) = 1$, $H(U_B|U_A) = 1$, $H(\hat{U}_{A\oplus B}|U_A, U_B) = H_b(p_e)$, and $H(\tilde{U}_{A\oplus B}|U_A, U_B, \hat{U}_{A\oplus B}) = H_b(p_d)$.

Moreover, we can also express $H(U_A, U_B, \hat{U}_{A\oplus B}, \tilde{U}_{A\oplus B})$ in the form of

$$H(U_A, U_B, \hat{U}_{A\oplus B}, \tilde{U}_{A\oplus B}) = H(\tilde{U}_{A\oplus B}) + H(U_A, U_B|\tilde{U}_{A\oplus B}) + H(\hat{U}_{A\oplus B}|U_A, U_B, \tilde{U}_{A\oplus B}), \quad (50)$$

where $H(\tilde{U}_{A\oplus B}) = 1$.

We have the following expression for the conditional mutual information,

$$\begin{aligned} I(\hat{U}_{A\oplus B}; \tilde{U}_{A\oplus B}|U_A, U_B) &= H(\hat{U}_{A\oplus B}|U_A, U_B) \\ &- H(\hat{U}_{A\oplus B}|U_A, U_B, \tilde{U}_{A\oplus B}) \\ &= H(\tilde{U}_{A\oplus B}|U_A, U_B) - H(\tilde{U}_{A\oplus B}|U_A, U_B, \hat{U}_{A\oplus B}). \end{aligned} \quad (51)$$

According to (51), we can get

$$H(\hat{U}_{A\oplus B}|U_A, U_B, \tilde{U}_{A\oplus B}) = H_b(p_e) + H_b(p_d) - H_b(p_e * p_d). \quad (52)$$

By combining (49), (50), and (52), we can obtain

$$H(U_A, U_B|\tilde{U}_{A\oplus B}) = 1 + H_b(p_e * p_d). \quad (53)$$

For the term $H(U_A|U_B, \tilde{U}_{A\oplus B})$ in (16), we can refer to the following derivation

$$H(U_A|U_B, \tilde{U}_{A\oplus B}) = H(U_A, U_B|\tilde{U}_{A\oplus B}) - H(U_B|\tilde{U}_{A\oplus B}), \quad (54)$$

where $H(U_B|\tilde{U}_{A\oplus B}) = 1$. Then, we get

$$H(U_A|U_B, \tilde{U}_{A\oplus B}) = H_b(p_e * p_d). \quad (55)$$

Due to the symmetry property of U_A and U_B , it is easy to get

$$H(U_B|U_A, \tilde{U}_{A\oplus B}) = H_b(p_e * p_d). \quad (56)$$

APPENDIX B DERIVATION OF (28)

For the purpose of better illustration, we set $\Theta(\gamma_{R,D}) = H_b(p_d)$, $\Gamma(\gamma_{A,R}) = H_b(p_e)$, $\Lambda(\gamma_{A,R}, \gamma_{R,D}) = H_b(p_e * p_d)$. The details of each components included in (28) are shown in (57)–(60). The coefficient “2” in (59) and (60) is due to the symmetry of the network topology. That is, the probabilities of \mathcal{R}_1 and \mathcal{R}_2 are equal and their impact on the outage probability is also equal.

APPENDIX C DERIVATION OF (37), (43), AND (46)

The *a priori* LLR in (37) can be expressed as

$$\begin{aligned} L_a(x_A^k) &= \ln \left(\frac{\sum_{i=\pm 1} \Pr(x_A^k = 1, x_B^k = i|y_{R,1}^k)}{\sum_{i=\pm 1} \Pr(x_A^k = -1, x_B^k = i|y_{R,1}^k)} \right) \\ &= \ln \left(\frac{\sum_{i=\pm 1} \Pr(y_{R,1}^k | x_A^k = 1, x_B^k = i) \Pr(x_A^k = 1, x_B^k = i)}{\sum_{i=\pm 1} \Pr(y_{R,1}^k | x_A^k = -1, x_B^k = i) \Pr(x_A^k = -1, x_B^k = i)} \right) \\ &\stackrel{(a)}{=} \ln \left(\frac{\sum_{i=\pm 1} \Pr(y_{R,1}^k | x_A^k = 1, x_B^k = i) \Pr(x_B^k = i)}{\sum_{i=\pm 1} \Pr(y_{R,1}^k | x_A^k = -1, x_B^k = i) \Pr(x_B^k = i)} \right), \end{aligned} \quad (61)$$

where (a) takes into consideration of x_B^k only in the joint probabilities. In (61), $\Pr(y_{R,1}^k | x_A^k = 1, x_B^k = i)$ and $\Pr(y_{R,1}^k | x_A^k = -1, x_B^k = i)$ follow Gaussian distribution. Also, we know that $L_e(x_B^k) = \ln(\Pr(x_B^k = 1)/\Pr(x_B^k = -1))$. After some manipulations, we can get the final expression of $L_a(x_A^k)$ in (37).

In the derivation of (43), we first calculate the two probabilities, i.e., $\Pr(u_A^k = 0)$ and $\Pr(u_A^k = 1)$, and then take the ln operation on the ratio $\Pr(u_A^k = 0)/\Pr(u_A^k = 1)$.

$$\begin{aligned} \Pr(u_A^k = 0) &\stackrel{(a)}{=} \Pr(u_A^k = 0|u_B^k = 0, u_R^k = 0)\Pr(u_B^k = 0, u_R^k = 0) \\ &+ \Pr(u_A^k = 0|u_B^k = 1, u_R^k = 1)\Pr(u_B^k = 1, u_R^k = 1) \\ &+ \Pr(u_A^k = 0|u_B^k = 0, u_R^k = 1)\Pr(u_B^k = 0, u_R^k = 1) \\ &+ \Pr(u_A^k = 0|u_B^k = 1, u_R^k = 0)\Pr(u_B^k = 1, u_R^k = 0) \\ &\stackrel{(b)}{=} (1 - \hat{p}_e)\Pr(u_B^k = 0, u_R^k = 0) \\ &+ (1 - \hat{p}_e)\Pr(u_B^k = 1, u_R^k = 1) \\ &+ \hat{p}_e\Pr(u_B^k = 0, u_R^k = 1) + \hat{p}_e\Pr(u_B^k = 1, u_R^k = 0) \\ &\stackrel{(c)}{=} (1 - \hat{p}_e)\Pr(u_B^k = 0)\Pr(u_R^k = 0)(1 - \hat{p}_u) \\ &+ (1 - \hat{p}_e)\Pr(u_B^k = 1)\Pr(u_R^k = 1)\hat{p}_u \\ &+ \hat{p}_e\Pr(u_B^k = 0)\Pr(u_R^k = 1)(1 - \hat{p}_u) \\ &+ \hat{p}_e\Pr(u_B^k = 1)\Pr(u_R^k = 0)\hat{p}_u, \end{aligned} \quad (62)$$

where (a) follows Bayes' rules; (b) is derived by using $\Pr(u_A^k = 0|u_B^k = 0, u_R^k = 0) = \Pr(u_A^k = 0|u_B^k = 1, u_R^k = 1) = (1 - \hat{p}_e)$ and $\Pr(u_A^k = 0|u_B^k = 0, u_R^k = 1) = \Pr(u_A^k = 0|u_B^k = 1, u_R^k = 0) = \hat{p}_e$; Note that we use the estimate of p_e in the derivation instead of p_e ; (c) follows Eqs. (8) and (9) in [6]. Similarly, we can get the expression for $\Pr(u_A^k = 1)$. Considering $L_e(u_B^k) = \ln(\Pr(u_B^k = 0)/\Pr(u_B^k = 1))$ and $L_e(u_R^k) = \ln(\Pr(u_R^k = 0)/\Pr(u_R^k = 1))$ and taking ln on $\Pr(u_A^k = 0)/\Pr(u_A^k = 1)$, we get the final expression of $L_a(x_A^k)$ in (43).

The estimate of p_e is shown in (63). Then, both numerator and denominator are divided by $\Pr(u_A^k = 1)\Pr(u_B^k = 1)\Pr(u_R^k = 1)$. Considering $L_p(u_A^k) = \ln(\Pr(u_A^k = 0)/\Pr(u_A^k = 1))$, $L_p(u_B^k) = \ln(\Pr(u_B^k = 0)/\Pr(u_B^k = 1))$, and $L_p(u_R^k) = \ln(\Pr(u_R^k = 0)/\Pr(u_R^k = 1))$, we get the part on the right side of summation in (46). After taking average over the information length K , we get the final expression, shown in (46).

REFERENCES

- [1] X. Zhou, M. Cheng, X. He, and T. Matsumoto, “Exact and approximated outage probability analyses for decode-and-forward relaying system allowing intra-link errors,” *IEEE Trans. Wireless Commun.*, vol. 13, no. 12, pp. 7062–7071, Dec. 2014.
- [2] Y. Zhao, R. Adve, and T. J. Lim, “Outage probability at arbitrary SNR with cooperative diversity,” *IEEE Commun. Lett.*, vol. 9, no. 8, pp. 700–702, Aug. 2005.
- [3] N. Beaulieu and J. Hu, “A closed-form expression for the outage probability of decode-and-forward relaying in dissimilar rayleigh fading channels,” *IEEE Commun. Lett.*, vol. 10, no. 12, pp. 813–815, Dec. 2006.
- [4] P. Popovski and H. Yomo, “Physical network coding in two-way wireless relay channels,” in *Proc. of IEEE ICC*, Jun. 2007, pp. 707–712.
- [5] T. Koike-Akino, P. Popovski, and V. Tarokh, “Optimized constellations for two-way wireless relaying with physical network coding,” *IEEE Journal on Selected Areas in Communications*, vol. 27, no. 5, pp. 773–787, Jun. 2009.
- [6] X. Zhou, P.-S. Lu, K. Anwar, and T. Matsumoto, “Correlated sources transmission in orthogonal multiple access relay channel: Theoretical analysis and performance evaluation,” *IEEE Trans. Wireless Commun.*, vol. 13, no. 3, pp. 1424–1435, Mar. 2014.
- [7] D. H. Woldegebreel and H. Karl, “Multiple-access relay channel with network coding and non-ideal source-relay channels,” in *Proc. of ISWCS*, Oct. 2007, pp. 732–736.
- [8] P.-S. Lu, X. Zhou, and T. Matsumoto, “Outage probabilities of orthogonal multiple-access relaying techniques with imperfect source-relay links,” *IEEE Trans. Wireless Commun.*, vol. 14, no. 4, pp. 2269–2280, Apr. 2015.

$$\begin{aligned}
\Pr\{S|C_1\}\Pr\{C_1\} &= \int_{\mathbb{V}_1} \cdots \int p(\gamma_{A,R})p(\gamma_{B,R})p(\gamma_{R,D})p(\gamma_{A,D})p(\gamma_{B,D})d\gamma_{A,R}d\gamma_{B,R}d\gamma_{R,D}d\gamma_{A,D}d\gamma_{B,D} \\
&= \left[\int_{\Phi^{-1}(1)}^{\infty} p(\gamma_{B,R})d\gamma_{B,R} \int_{\Phi^{-1}(1)(1+\gamma_{B,R})}^{\infty} p(\gamma_{A,R})d\gamma_{A,R} + \int_{\Phi^{-1}(1)}^{[\Phi^{-1}(1)+\Phi^{-1}(1)\Phi^{-1}(2)]/[1+\Phi^{-1}(1)]} p(\gamma_{A,R})d\gamma_{A,R} \int_{\Phi^{-1}(2)-\gamma_{A,R}}^{\infty} p(\gamma_{B,R})d\gamma_{B,R} \right. \\
&\quad \left. + \int_{[\Phi^{-1}(1)+\Phi^{-1}(1)\Phi^{-1}(2)]/[1+\Phi^{-1}(1)]}^{\infty} p(\gamma_{A,R})d\gamma_{A,R} \int_{\gamma_{A,R}/\Phi^{-1}(1)-1}^{\infty} p(\gamma_{B,R})d\gamma_{B,R} \right] \\
&\times \left[\int_{\Phi^{-1}(1)}^{\infty} p(\gamma_{R,D})d\gamma_{R,D} \int_{\Phi^{-1}(0)}^{\Phi^{-1}(1)} p(\gamma_{A,D})d\gamma_{A,D} \int_{\Phi^{-1}(1)-\gamma_{A,D}}^{\infty} p(\gamma_{B,D})d\gamma_{B,D} \right. \\
&\quad \left. + \int_{\Phi^{-1}(1)}^{\infty} p(\gamma_{R,D})d\gamma_{R,D} \int_{\Phi^{-1}(1)}^{\infty} p(\gamma_{A,D})d\gamma_{A,D} \int_0^{\infty} p(\gamma_{B,D})d\gamma_{B,D} \right], \tag{57}
\end{aligned}$$

$$\begin{aligned}
\Pr\{S|C_2\}\Pr\{C_2\} &= \int_{\mathbb{V}_2} \cdots \int p(\gamma_{A,R})p(\gamma_{B,R})p(\gamma_{R,D})p(\gamma_{A,D})p(\gamma_{B,D})d\gamma_{A,R}d\gamma_{B,R}d\gamma_{R,D}d\gamma_{A,D}d\gamma_{B,D} \\
&= \left[\int_{\Phi^{-1}(1)}^{\infty} p(\gamma_{B,R})d\gamma_{B,R} \int_{\Phi^{-1}(1)(1+\gamma_{B,R})}^{\infty} p(\gamma_{A,R})d\gamma_{A,R} + \int_{\Phi^{-1}(1)}^{[\Phi^{-1}(1)+\Phi^{-1}(1)\Phi^{-1}(2)]/[1+\Phi^{-1}(1)]} p(\gamma_{A,R})d\gamma_{A,R} \int_{\Phi^{-1}(2)-\gamma_{A,R}}^{\infty} p(\gamma_{B,R})d\gamma_{B,R} \right. \\
&\quad \left. + \int_{[\Phi^{-1}(1)+\Phi^{-1}(1)\Phi^{-1}(2)]/[1+\Phi^{-1}(1)]}^{\infty} p(\gamma_{A,R})d\gamma_{A,R} \int_{\gamma_{A,R}/\Phi^{-1}(1)-1}^{\infty} p(\gamma_{B,R})d\gamma_{B,R} \right] \\
&\times \left[\int_{\Phi^{-1}(0)}^{\Phi^{-1}(1)} p(\gamma_{R,D})d\gamma_{R,D} \int_{\Phi^{-1}[\Theta(\gamma_{R,D})]}^{\Phi^{-1}(1)} p(\gamma_{A,D})d\gamma_{A,D} \int_{\Phi^{-1}[1+\Theta(\gamma_{R,D})]-\gamma_{A,D}}^{\infty} p(\gamma_{B,D})d\gamma_{B,D} \right. \\
&\quad \left. + \int_{\Phi^{-1}(0)}^{\Phi^{-1}(1)} p(\gamma_{R,D})d\gamma_{R,D} \int_{\Phi^{-1}(1)}^{\infty} p(\gamma_{A,D})d\gamma_{A,D} \int_{\Phi^{-1}[\Theta(\gamma_{R,D})]}^{\infty} p(\gamma_{B,D})d\gamma_{B,D} \right], \tag{58}
\end{aligned}$$

$$\begin{aligned}
\Pr\{S|C_3\}\Pr\{C_3\} &= \int_{\mathbb{V}_3} \cdots \int p(\gamma_{A,R})p(\gamma_{B,R})p(\gamma_{R,D})p(\gamma_{A,D})p(\gamma_{B,D})d\gamma_{A,R}d\gamma_{B,R}d\gamma_{R,D}d\gamma_{A,D}d\gamma_{B,D} \\
&= 2 \times \int_{\Phi^{-1}(1)}^{\infty} p(\gamma_{B,R})d\gamma_{B,R} \int_0^{\Phi^{-1}(1)(1+\gamma_{B,R})} p(\gamma_{A,R})d\gamma_{A,R} \\
&\times \left[\int_{\Phi^{-1}(1)}^{\infty} p(\gamma_{R,D})d\gamma_{R,D} \int_{\Phi^{-1}[\Gamma(\gamma_{A,R})]}^{\Phi^{-1}(1)} p(\gamma_{A,D})d\gamma_{A,D} \int_{\Phi^{-1}[1+\Gamma(\gamma_{A,R})]-\gamma_{A,D}}^{\infty} p(\gamma_{B,D})d\gamma_{B,D} \right. \\
&\quad \left. + \int_{\Phi^{-1}(1)}^{\infty} p(\gamma_{R,D})d\gamma_{R,D} \int_{\Phi^{-1}(1)}^{\infty} p(\gamma_{A,D})d\gamma_{A,D} \int_{\Phi^{-1}[\Gamma(\gamma_{A,R})]}^{\infty} p(\gamma_{B,D})d\gamma_{B,D} \right], \tag{59}
\end{aligned}$$

$$\begin{aligned}
\Pr\{S|C_4\}\Pr\{C_4\} &= \int_{\mathbb{V}_4} \cdots \int p(\gamma_{A,R})p(\gamma_{B,R})p(\gamma_{R,D})p(\gamma_{A,D})p(\gamma_{B,D})d\gamma_{A,R}d\gamma_{B,R}d\gamma_{R,D}d\gamma_{A,D}d\gamma_{B,D} \\
&= 2 \times \int_{\Phi^{-1}(1)}^{\infty} p(\gamma_{B,R})d\gamma_{B,R} \int_0^{\Phi^{-1}(1)(1+\gamma_{B,R})} p(\gamma_{A,R})d\gamma_{A,R} \\
&\times \left[\int_{\Phi^{-1}(0)}^{\Phi^{-1}(1)} p(\gamma_{R,D})d\gamma_{R,D} \int_{\Phi^{-1}[\Lambda(\gamma_{A,R},\gamma_{R,D})]}^{\Phi^{-1}(1)} p(\gamma_{A,D})d\gamma_{A,D} \int_{\Phi^{-1}[1+\Lambda(\gamma_{A,R},\gamma_{R,D})]-\gamma_{A,D}}^{\infty} p(\gamma_{B,D})d\gamma_{B,D} \right. \\
&\quad \left. + \int_{\Phi^{-1}(0)}^{\Phi^{-1}(1)} p(\gamma_{R,D})d\gamma_{R,D} \int_{\Phi^{-1}(1)}^{\infty} p(\gamma_{A,D})d\gamma_{A,D} \int_{\Phi^{-1}[\Lambda(\gamma_{A,R},\gamma_{R,D})]}^{\infty} p(\gamma_{B,D})d\gamma_{B,D} \right]. \tag{60}
\end{aligned}$$

$$\begin{aligned}
\hat{p}_e &= \Pr(u_A^k = 0)\Pr(u_B^k = 0)\Pr(u_R^k = 1) + \Pr(u_A^k = 0)\Pr(u_B^k = 1)\Pr(u_R^k = 0) \\
&+ \Pr(u_A^k = 1)\Pr(u_B^k = 0)\Pr(u_R^k = 0) + \Pr(u_A^k = 1)\Pr(u_B^k = 1)\Pr(u_R^k = 1) \\
&= \frac{\Pr(u_A^k = 0)\Pr(u_B^k = 0)\Pr(u_R^k = 1) + \Pr(u_A^k = 0)\Pr(u_B^k = 1)\Pr(u_R^k = 0)}{\left[\Pr(u_A^k = 0) + \Pr(u_A^k = 1)\right] \left[\Pr(u_B^k = 0) + \Pr(u_B^k = 1)\right] \left[\Pr(u_R^k = 0) + \Pr(u_R^k = 1)\right]} \\
&+ \frac{\Pr(u_A^k = 1)\Pr(u_B^k = 0)\Pr(u_R^k = 0) + \Pr(u_A^k = 1)\Pr(u_B^k = 1)\Pr(u_R^k = 1)}{\left[\Pr(u_A^k = 0) + \Pr(u_A^k = 1)\right] \left[\Pr(u_B^k = 0) + \Pr(u_B^k = 1)\right] \left[\Pr(u_R^k = 0) + \Pr(u_R^k = 1)\right]}
\end{aligned} \tag{63}$$

- [9] Y. Li, G. Song, and L. Wang, "Design of joint network-low density parity check codes based on the EXIT charts," *IEEE Commun. Lett.*, vol. 13, no. 8, pp. 600–602, Aug. 2009.
- [10] P.-S. Lu, X. Zhou, K. Anwar, and T. Matsumoto, "Joint adaptive network-channel coding for energy-efficient multiple-access relaying," *IEEE Trans. Veh. Technol.*, vol. 63, no. 5, pp. 2298–2305, Jun. 2014.
- [11] C. Hausl and P. Dupraz, "Joint network-channel coding for the multiple-access relay channel," in *proc. of IEEE Communications Society on Sensor and Ad Hoc Communications and Networks*, vol. 3, Sep 2006, pp. 817–822.
- [12] E. Paolini, C. Stefanovic, G. Liva, and P. Popovski, "Coded random access: applying codes on graphs to design random access protocols," *IEEE Commun. Mag.*, vol. 53, no. 6, pp. 144–150, Jun. 2015.
- [13] Z. Zhang, C. Xu, and L. Ping, "Coded random access with distributed power control and multiple-packet reception," *IEEE Wireless Commun. Lett.*, vol. 4, no. 2, pp. 117–120, Apr. 2015.
- [14] J. He, I. Hussain, M. Juntti, and T. Matsumoto, "Transmission of correlated sources over non-orthogonal Gaussian MACs," in *Proc. of IEEE ICC Workshops*, May 2016, pp. 534–539.
- [15] K. Anwar and T. Matsumoto, "Iterative spatial demapping for two correlated sources with power control over fading MAC," in *Proc. of IEEE VTC*, May 2012, pp. 1–7.
- [16] J. He, I. Hussain, V. Tervo, M. Juntti, and T. Matsumoto, "Performance analysis for transmission of correlated sources over non-orthogonal MARCs," in *Proc. of International Symposium on Turbo Codes and Iterative Information Processing (ISTC)*, Sept 2016, pp. 66–70.
- [17] L. Ping, L. Liu, K. Wu, and W. K. Leung, "Interleave division multiple-access," *IEEE Trans. Wireless Commun.*, vol. 5, no. 4, pp. 938–947, Apr. 2006.
- [18] J. Tong and L. Ping, "Performance analysis of superposition coded modulation," *Physical Communication*, vol. 3, no. 3, pp. 147 – 155, 2010.
- [19] P. Chen, S. C. Liew, and L. Shi, "Bandwidth-efficient coded modulation schemes for physical-layer network coding with high-order modulations," *IEEE Trans. Commun.*, vol. 65, no. 1, pp. 147–160, Jan 2017.
- [20] T. Cover and A. E. Gamal, "Capacity theorems for the relay channel," *IEEE Trans. Inf. Theory*, vol. 25, no. 5, pp. 572–584, Sep 1979.
- [21] J. N. Laneman and G. W. Wornell, "Distributed space-time-coded protocols for exploiting cooperative diversity in wireless networks," *IEEE Trans. Inf. Theory*, vol. 49, no. 10, pp. 2415–2425, Oct 2003.
- [22] J. N. Laneman, D. N. C. Tse, and G. W. Wornell, "Cooperative diversity in wireless networks: Efficient protocols and outage behavior," *IEEE Trans. Inf. Theory*, vol. 50, no. 12, pp. 3062–3080, Dec 2004.
- [23] G. Kramer, M. Gastpar, and P. Gupta, "Cooperative strategies and capacity theorems for relay networks," *IEEE Trans. Inf. Theory*, vol. 51, no. 9, pp. 3037–3063, Sep 2005.
- [24] A. Bletsas, H. Shin, and M. Z. Win, "Cooperative communications with outage-optimal opportunistic relaying," *IEEE Trans. Wireless Commun.*, vol. 6, no. 9, pp. 3450–3460, September 2007.
- [25] 3GPP Technical Report 36.814. V2.0.1., "Further advancements for E-UTRA physical layer aspects," Mar 2010.
- [26] D. C. Gonzalez, A. Wolf, L. L. Mendes, J. C. S. S. Filho, and G. Fettweis, "An efficient power allocation scheme for multirelay systems with lossy intra-links," *IEEE Trans. Commun.*, vol. PP, no. 99, pp. 1–1, 2017.
- [27] A. El Gamal and Y.-H. Kim, *Network information theory*. Cambridge university press, 2011.
- [28] X. Zhou, X. He, M. Juntti, and T. Matsumoto, "Outage probability of correlated binary source transmission over fading multiple access channels," in *Proc. of IEEE SPAWC*, Jun. 2015, pp. 96–100.
- [29] R. Narasimhan, "Individual outage rate regions for fading multiple access channels," in *Proc. of IEEE ISIT*, Jun. 2007, pp. 1571–1575.
- [30] G. Ungerboeck, "Channel coding with multilevel/phase signals," *IEEE Trans. Inf. Theory*, vol. 28, no. 1, pp. 55–67, Jan 1982.
- [31] X. Zhou, M. Cheng, K. Anwar, and T. Matsumoto, "Distributed joint source-channel coding for relay systems exploiting source-relay correlation and source memory," *EURASIP Journal on Wireless Communications and Networking*, vol. 2012, no. 1, p. 260, 2012.
- [32] L. You, S. C. Liew, and L. Lu, "Network-coded multiple access II: Toward real-time operation with improved performance," *IEEE J. Sel. Areas Commun.*, vol. 33, no. 2, pp. 264–280, Feb. 2015.
- [33] L. Bahl, J. Cocke, F. Jelinek, and J. Raviv, "Optimal decoding of linear codes for minimizing symbol error rate," *IEEE Trans. Inf. Theory*, vol. 20, no. 2, pp. 284–287, Mar 1974.
- [34] K. Anwar and T. Matsumoto, "Accumulator-assisted distributed turbo codes for relay systems exploiting source-relay correlation," *IEEE Commun. Lett.*, vol. 16, no. 7, pp. 1114–1117, Jul. 2012.
- [35] O. Y. Takeshita and D. J. Costello, "New deterministic interleaver designs for turbo codes," *IEEE Trans. Inf. Theory*, vol. 46, no. 6, pp. 1988–2006, Sep. 2000.
- [36] R. Youssef and A. G. i. Amat, "Distributed serially concatenated codes for multi-source cooperative relay networks," *IEEE Trans. Wireless Commun.*, vol. 10, no. 1, pp. 253–263, Jan. 2011.