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Description	



Age-of-Information in First-Come-First-Served Wireless Communications: Upper Bound and Performance Optimization

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Abstract—This paper establishes an analytical framework for the upper bound on the average Age-of-Information (AoI) in first-come-first-served (FCFS) wireless communications where a certain level of outage probability is unavoidable. To begin with, we analyze the average AoI and derive a general upper bound for G/G/1 systems with a certain outage probability. Subsequently, for an M/M/1 system with the FCFS scheme, we obtain a concise closed-form expression of the upper bound, and further refine the upper bound after analyzing the relative error. Interestingly, it is found by the analysis that the relative error is independent of the service rate, and the upper bound becomes tighter as the outage probability increases. Based on the refined upper bound, we minimize the average AoI for the communications suffering from block Rayleigh fading. We derive a closed-form expression of the outage probability over a fading channel, and then prove that the refined upper bound is a convex function with respect to the average update generating rate. Consequently, we optimize the AoI performance by solving a convex optimization problem formulated utilizing the refined upper bound expression. The numerical results indicate that the minimum average AoI can be reduced by either increasing the service rate or the transmission power.

Index Terms—Age-of-Information, outage probability, first-come-first-served, G/G/1 systems, M/M/1 systems.

I. INTRODUCTION

Age-of-Information (AoI) [1] is a reasonable metric indicating the dynamics of information freshness. Kaul *et al.* proposed the concept of AoI for the first time in [2], where AoI is introduced for designing transmission strategy in vehicular

networks. The general definition of AoI is the elapsed time of the latest successfully updated information since the information is generated. Compared to static metrics such as delay and latency, AoI better reflects the variation of the information freshness along with time. Therefore, the concept of AoI has been widely adopted in various areas of network design as the key metric for performance analysis and/or algorithm design [3]–[7].

Nowadays, mobile devices have been and will be rapidly increasing as reported in [8], especially as Internet-of-Things (IoT) spreads over the world. The wireless transmissions may fail if the system suffers from severe fading and interference, resulting in the outage events which cannot be completely avoided because propagation of the electronic-magnetic waves is a natural phenomenon. Furthermore, in wireless IoT networks massive devices are assumed to be connected. Therefore, when using AoI as a metric for evaluating the performance of the wireless IoT networks, not only the latency due to the elapsed time in the queue but also the outage probability of the wireless links suffering from the fading variation, have to be taken into account. Once an outage event occurs, AoI increases continuously due to the failure of updating information. For the purpose of analyzing AoI in wireless communication networks, we need to establish a mathematical relationship between the outage probability and the average AoI.

In the IoT era, a lot of wireless devices rely on battery rather than power supply line during most of time (in fact, assuming power supply line contradicts wireless communications, because they can also guarantee reliable wired communications by cables). Hence, there is a constraint on the total transmission energy during a specific time interval for wireless devices. Then, an interesting trade-off appears, i.e., the system can increase the generating rate of updates to reduce AoI; however, more updates decrease the average transmission power and increase the outage probability, which causes larger AoI. To achieve the best trade-off between the generating rate of updates and the transmission power, it is necessary to derive the outage probability for a given transmission power in addition to the average AoI with a certain outage probability.

To date, there is some research work related to AoI analysis considering packet errors with a certain outage probability. The peak AoI for the M/M/1 system was characterized for the first-come-first-served (FCFS) or last-come-first-served (LCFS) scheme by Chen and Huang in [9]. Arafa *et al.* [10] analyzed the average AoI in energy harvesting communications where energy arrives according to a Poisson process and a status update is served immediately. Kam *et al.* [11] studied the average AoI for an M/M/1/2 system where the outage event is

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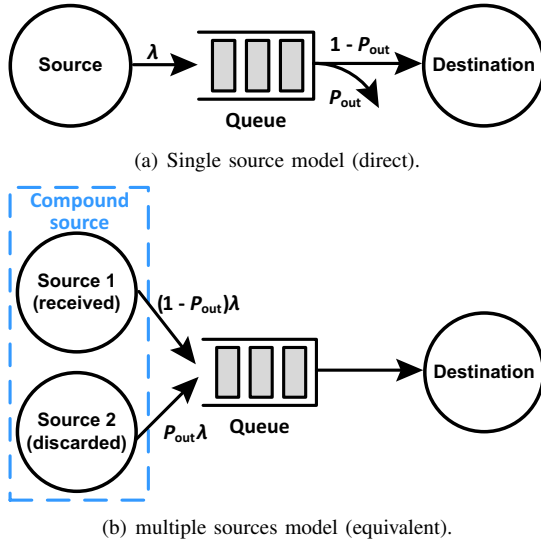


Fig. 1. Two ways to analyzing the AoI in communications with outages.

controlled by a packet deadline. Zhang *et al.* [12] minimized the total AoI by joint sensing and transmission optimization, taking into account the successful sensing probability. Lin *et al.* [13] derived a lower bound on the average AoI for the M/M/1 system with a given outage probability. Ling *et al.* [14] minimized the average discrete AoI in healthcare IoT with the outage probabilities of energy harvesting and information transmissions.

Nonetheless, it is not easy to obtain an exact expression of the average AoI for the general queueing model (i.e., the G/G/1 system) with the FCFS scheme, due to the complicated stochastic properties and the infinite queue length in various queueing models. The complicated calculation of the exact average AoI may hinder the practical implementation of some algorithms based on AoI. Therefore, the objective of this paper is to find a concise approximation (i.e., an upper bound) of the average AoI for G/G/1 systems with the FCFS scheme. By utilizing the upper bound, we can reduce the computation cost for AoI optimization while keeping the reasonable accuracy of the performance evaluation.

There are two ways to analyzing the AoI in wireless communications with outages, i.e., the direct and equivalent models as illustrated in Fig. 1(a) and Fig. 1(b), respectively. In the direct model, the source has an arrival rate λ , and the queue has a packet discard probability P_{out} . In the equivalent model, two sources have the arrival rates $(1 - P_{out})\lambda$ and $P_{out}\lambda$, respectively. Hence, the arrival rate of the compound source is also equal to λ . If we only consider the AoI of Source 1 while ignoring Source 2, the result is equivalent to the direct model.

The previous results for the AoI analysis in the presence of multiple sources can be utilized for analyzing the AoI in communications with outages based on the equivalent model. Moltafet *et al.* [15] approximated the average AoI for the two sources M/G/1 system, which is equivalent to the system with outages by considering one of the sources as the discarded packet. Kaul and Yates [16] derived the average AoI for one

of the sources in the multi-source M/M/1 system. Huang and Modiano [17] characterized the peak AoI for the two sources M/G/1 system.

However, a fundamental problem, arising when using the equivalent model, is how to construct the probability density functions (PDFs) of the information generation time interval for two sources, such that the PDF for the compound source is the same as the PDF for the source in the direct model. It is difficult to construct the PDFs for two sources unless the compound source follows a Poisson process. Due to the complexity of constructing the PDFs for two sources in G/G/1 systems, this paper analyzes AoI based on the direct model.

For the calculation of the outage probability, the scenario can be roughly classified into two categories: lossless and lossy communications. Actually, lossy communications reduce to lossless when the distortion requirement becomes 0, i.e., the recovered information is exactly the same as the source information. Hence, to make the results more generic, we derive the outage probability for lossy communications in this paper. The basic principle for the derivation of the outage probability is to calculate the probability of the instantaneous channel capacities less than the achievable capacities. Since the system models of cooperative communications have much more variety than that of point-to-point communications, the previous results regarding the outage probability are almost for cooperative communications. For example, Kramer *et al.* [18] determined the outage probability of lossless decode-and-forward (DF) relaying systems. As presented in [19]–[22], there were also a lot of work related to the outage probability analyses of lossless communications assisted by lossy-forward (LF) [23] relaying over block Rayleigh fading channels. Regarding end-to-end lossy communications, the outage probability was investigated for correlated binary sources in [24], [25].

Nevertheless, most of the previous work focuses on the outage probability for end-to-end lossless communications. Besides, the work for lossy communications analyzes the outage probability by numerical solutions instead of analytical solutions. Therefore, we aim at deriving a closed-form expression of the outage probability for lossy communications with a Gaussian source in this paper. By this means, we can further mathematically prove the optimality of the trade-off between the generating rate of updates and the transmission power for minimizing AoI.

Compared to the literature, this paper derives the upper bound on the average AoI for G/G/1 systems with the FCFS scheme, and determines the outage probability for lossy communications with a Gaussian source. Based on the closed-form expressions of the upper bound and the outage probability, the AoI performance is optimized for the system with an energy budget constraint. The contributions of this paper are summarized as follows:

- We establish an analytical framework for evaluating the average AoI for FCFS wireless communications with outages. Specifically, we derive an upper bound on the average AoI for the G/G/1 systems representing the most generic one-server queue model, given a required outage probability.

- We determine the upper bound on the average AoI for the M/M/1 system, and present a concise closed-form expression of the upper bound.
- We evaluate the relative error of the upper bound between the approximated and exact average AoI, and further propose a refined upper bound with a concise closed-form expression. The numerical results imply that the relative error is a function of the outage probability and the server utilization ratio.
- Based on the Shannon's lossy source-channel separation theorem [26], [27], we obtain a closed-form expression of the outage probability for point-to-point lossy communications with a Gaussian source over a block Rayleigh fading channel.
- Finally, we prove that the refined upper bound on the average AoI is a convex function with respect to the update generating rate. Hence, by utilizing the refined upper bound, the problem of minimizing the average AoI can be solved by the convex optimization framework. The numerical results demonstrate that the increment of the service rate or the transmission power efficiently reduces the minimum average AoI when they are within a relatively small range.

The rest of this paper is organized as follows. Section II establishes the analytical framework of the upper bound on the average AoI for FCFS communications with a certain level of outage probability. Section III derives an upper bound and refines the upper bound for the M/M/1 system. Section IV focuses on the AoI optimization for lossy communications with a Gaussian source over a block Rayleigh fading channel. Finally, we conclude this work in Section V.

II. ANALYTICAL FRAMEWORK OF AOI IN G/G/1 SYSTEMS

This section establishes the analytical framework of the average AoI and derives the upper bound for G/G/1 systems with a given outage probability.

We start with a brief review of the basic analytical framework on the average AoI for the G/G/1 system with the FCFS scheme in Section II-A. Then, we make an in-depth investigation on the dynamics of AoI when outage events occur in Section II-B. Section II-C presents a general upper bound on the average AoI with a given outage probability requirement.

A. Basic Analytical Framework

Fig. 2 depicts the dynamics of AoI along with time elapsing for reliable communications. The i -th update is generated and its service is completed at the time of t_i and t'_i , respectively. Therefore, $Y_i = t_i - t_{i-1}$ is the interarrival time between the $(i-1)$ -th and the i -th updates. Moreover, the system time $T_i = t'_i - t_i$ is the period of time for the i -th update staying in the system. From the view of queueing process, the system time T_i is the sum of the waiting time W_i in the queue and the service time S_i , i.e., $T_i = W_i + S_i$. The i -th update has to wait from t_i to t'_{i-1} , if it is generated before the system finishes the service of the $(i-1)$ -th update; otherwise, the waiting time in the queue for the i -th update is 0. Hence, $W_i = (t'_{i-1} - t_i)^+ = (T_{i-1} - Y_i)^+$, where $(\cdot)^+ = \max(\cdot, 0)$.

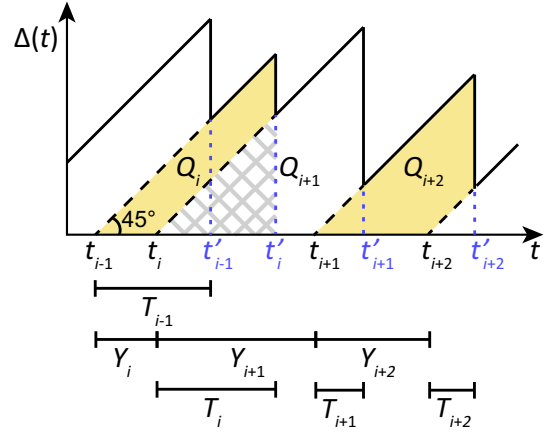


Fig. 2. The basic analytical framework of AoI for reliable communications.

Since the AoI $\Delta(t)$ is defined as the elapsed time of the latest served update from its generation, AoI will linearly increase along with time t with a gradient of 1. The average AoI for an interval $(0, \mathcal{T})$ can be calculated by

$$\Delta_{\mathcal{T}} = \frac{1}{\mathcal{T}} \int_0^{\mathcal{T}} \Delta(t) dt, \quad (1)$$

where the integral is equal to the area under $\Delta(t)$. As $\mathcal{T} \rightarrow \infty$, $\Delta_{\mathcal{T}}$ converges into the average AoI Δ for the system in stable states. By decomposing the area under $\Delta(t)$ into the trapezoids with their area being Q_i , the average AoI Δ can be calculated as the expectation of Q divided by the expectation of Y [28, Eq. (2.12)], i.e., $\Delta = \frac{E[Q]}{E[Y]}$. The area Q_i of a trapezoid is equal to the difference between two triangles, i.e.,

$$Q_i = \frac{1}{2}(Y_i + T_i)^2 - \frac{1}{2}T_i^2 = Y_i T_i + \frac{1}{2}Y_i^2. \quad (2)$$

Hence, we have

$$\Delta = \frac{E[YT] + E[Y^2]/2}{E[Y]}. \quad (3)$$

B. AoI with Outage Events

Now, we start the analysis of the AoI dynamics for the system where the outage events occur. As illustrated in Fig. 3, we consider the general case where the outage events occur k times successively. In this case, $\Delta(t)$ monotonically increases from t'_{i-1} to t'_{i+k} , and the system completes the service at the timing for the $(k+1)$ updates. Similar to the basic analytical framework of AoI for reliable communications, we can calculate the average AoI with k outage events by defining auxiliary variables

$$\tilde{Y}_i = \sum_{j=i}^{i+k} Y_j, \quad (4)$$

$$\tilde{T}_i = T_{i+k}. \quad (5)$$

Then, the area \tilde{Q}_i of the trapezoid with k outage events can be calculated by

$$\tilde{Q}_i = \tilde{Y}_i \tilde{T}_i + \frac{1}{2} \tilde{Y}_i^2, \quad (6)$$

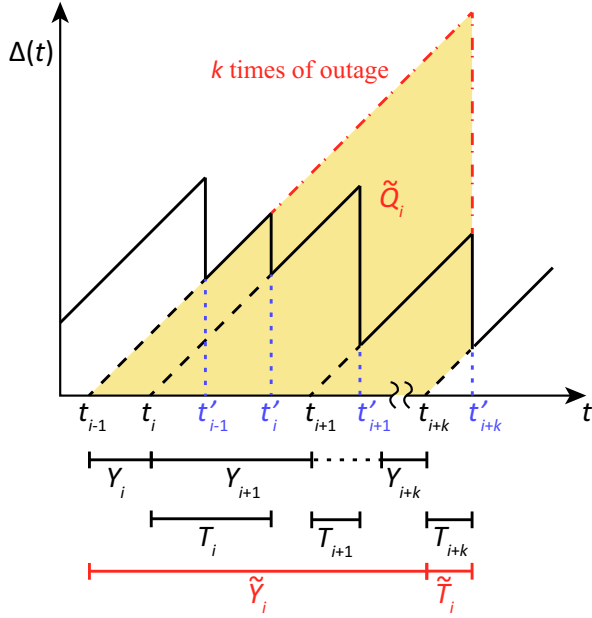


Fig. 3. The analytical framework of AoI with outage events.

and we can obtain the average AoI with k outage events as

$$\Delta_{(k)} = \frac{\mathbb{E}[\tilde{Q}]}{\mathbb{E}[\tilde{Y}]} = \frac{\mathbb{E}[\tilde{Y}\tilde{T}] + \mathbb{E}[\tilde{Y}^2]/2}{\mathbb{E}[\tilde{Y}]}, \quad (7)$$

with

$$\mathbb{E}[\tilde{Y}\tilde{T}] = \sum_{j=i}^{i+k} \mathbb{E}[Y_j W_{i+k}] + (k+1)\mathbb{E}[Y]\mathbb{E}[S], \quad (8)$$

$$\mathbb{E}[\tilde{Y}^2] = (k+1)(\mathbb{E}[Y^2] + k(\mathbb{E}[Y])^2), \quad (9)$$

$$\mathbb{E}[\tilde{Y}] = (k+1)\mathbb{E}[Y]. \quad (10)$$

The calculations for (8)-(10) are presented in Appendix A.

Subsequently, given an outage probability, the average AoI of the overall system can be calculated by the following proposition.

Proposition 1: The average AoI of the overall system with an outage probability P_{out} is

$$\Delta = (1 - P_{\text{out}})^2 \sum_{k=0}^{\infty} P_{\text{out}}^k (k+1) \Delta_{(k)}. \quad (11)$$

The proof of *Proposition 1* is presented in Appendix B.

From (7)-(10), we can find that the key to the calculation of the average AoI Δ is to determine $\mathbb{E}[Y_j W_{i+k}]$ in (8), since all other terms can be easily calculated given a specified queueing model. By contrast, Y_j and W_{i+k} are not independent for $j \leq i+k$ in general. Because the j -th update is generated earlier if the interarrival Y_j decreases, and hence the $(i+k)$ -th update also arrives earlier. However, the system requires the same time to finish the services of the updates, resulting in longer waiting time W_{i+k} . Therefore, W_{i+k} has a higher probability to be larger for smaller Y_j . Since it is difficult to obtain the conditional PDF of W_{i+k} for given y_j (i.e., an instance of the random variable Y_j), we need to further

decompose $\mathbb{E}[Y_j W_{i+k}]$ for calculating the exact value of $\Delta_{(k)}$. Consider

$$\begin{aligned} \mathbb{E}[Y_j W_{i+k}] &= \mathbb{E}[Y_j (T_{i+k-1} - Y_{i+k})^+] \\ &= \mathbb{E}[Y_j (W_{i+k-1} + S_{i+k-1} - Y_{i+k})^+] \\ &= \mathbb{E}[Y_j ((T_{i+k-2} - Y_{i+k-1})^+ + S_{i+k-1} - Y_{i+k})^+] \\ &= \mathbb{E}[Y_j ((\dots ((T_{j-1} - Y_j)^+ + S_j - Y_{j+1})^+ + \dots)^+ \\ &\quad + S_{i+k-1} - Y_{i+k})^+], \end{aligned} \quad (12)$$

where all the variables in (12) are independent with each other, and (12) can be further calculated by the integral as

$$\begin{aligned} \mathbb{E}[Y_j W_{i+k}] &= \int_0^{\infty} \dots \int_0^{\infty} [y_j ((\dots ((t_{j-1} - y_j)^+ + s_j \\ &\quad - y_{j+1})^+ + \dots)^+ + s_{i+k-1} - y_{i+k})^+] \\ &\quad \cdot f_T(t_{j-1}) f_Y(y_{i+k}) \prod_{m=j}^{i+k-1} f_S(s_m) f_Y(y_m) \\ &\quad \cdot dt_{j-1} ds_j dy_j \dots ds_{i+k-1} dy_{i+k-1} dy_{i+k}. \end{aligned} \quad (13)$$

Notice that it is difficult to obtain a concise closed-form expression of (13). Alternatively, we can utilize numerical algorithms to calculate $\mathbb{E}[Y_j W_{i+k}]$.

For the purpose of AoI optimization, we derive an upper bound on the average AoI in the following. Here, we start with bounding $\Delta_{(k)}$. As derived above, the key to bounding $\Delta_{(k)}$ is to bound $\mathbb{E}[Y_j W_{i+k}]$, i.e., the term which is difficult to have a closed-form expression.

C. General Upper Bound

We introduce the key results related to the upper bound first by the following two propositions.

Proposition 2: $\mathbb{E}[Y_j W_{i+k}]$ is upper bounded by

$$\mathbb{E}[Y_j W_{i+k}] < \mathbb{E}[Y_j W_{i-1}]. \quad (14)$$

The proof of *Proposition 2* is presented in Appendix C.

Proposition 3: $\Delta_{(k)}$ is upper bounded by

$$\Delta_{(k)} < \Delta_{(k)}^{\text{UB}} = \mathbb{E}[T] + \frac{\mathbb{E}[Y^2]}{2\mathbb{E}[Y]} + \frac{k\mathbb{E}[Y]}{2}. \quad (15)$$

Proof. Consider

$$\mathbb{E}[Y_j W_{i-1}] = \mathbb{E}[Y_j] \mathbb{E}[W_{i-1}] = \mathbb{E}[Y] \mathbb{E}[W], \quad (16)$$

where (16) follows since $j > i-1$ and hence W_{i-1} is independent of Y_j . By substituting (14) and (16) into (8), we have

$$\begin{aligned} \mathbb{E}[\tilde{Y}\tilde{T}] &< \sum_{j=i}^{i+k} \mathbb{E}[Y] \mathbb{E}[W] + (k+1)\mathbb{E}[Y] \mathbb{E}[S] \\ &= (k+1)\mathbb{E}[Y] \mathbb{E}[W] + (k+1)\mathbb{E}[Y] \mathbb{E}[S] \\ &= (k+1)\mathbb{E}[Y] (\mathbb{E}[W] + \mathbb{E}[S]) \\ &= (k+1)\mathbb{E}[Y] \mathbb{E}[T]. \end{aligned} \quad (17)$$

Then, we combine (7), (9), (10) and (17) together to upper bound $\Delta_{(k)}$ as

$$\Delta_{(k)} < \frac{(k+1)\mathbb{E}[Y] \mathbb{E}[T] + (k+1)(\mathbb{E}[Y^2] + k(\mathbb{E}[Y])^2) / 2}{(k+1)\mathbb{E}[Y]}$$

$$= E[T] + \frac{E[Y^2]}{2E[Y]} + \frac{kE[Y]}{2}. \quad (18)$$

This finishes the proof of *Proposition 3*. \blacksquare

Consequently, we can substitute $\Delta_{(k)}^{\text{UB}}$ into (11) to obtain the upper bound on the average AoI for the system with outage events.

III. AOI ANALYSIS FOR M/M/1 SYSTEMS

In order to visually evaluate the AoI performance, we need to specify the queueing model of the system. Thus, we select the most fundamental model, i.e., the M/M/1 system for performance analysis. The arrival of updates follows a Poisson process with mean arrival rate λ , and the service time follows the exponential distribution with parameter μ . Section III-A derives a concise closed-form expression of the upper bound on the average AoI in the M/M/1 system with outage events for the first step. Subsequently, Section III-B evaluates the relative error of the upper bound, and then refines the upper bound. Finally, Section III-C presents the numerical results with respect to the upper bound.

A. Upper Bound Derivation

For better reference, we summarize the PDFs and the expectations of basic variables in the M/M/1 system with the FCFS scheme as follows.

- Since the arrival of updates follows a Poisson process with mean arrival rate λ , the interarrival Y follows the independent and identically distributed (i.i.d.) exponential distribution with parameter λ , i.e.,

$$f_Y(y) = \lambda e^{-\lambda y}, 0 \leq y, \quad (19)$$

$$E[Y] = \frac{1}{\lambda}. \quad (20)$$

- The PDF and the expectation of the system time T are given by [29, Eq. (16-97), (16-98)]

$$f_T(t) = \mu(1 - \rho)e^{-\mu(1-\rho)t} = (\mu - \lambda)e^{-(\mu-\lambda)t}, 0 \leq t, \quad (21)$$

$$E[T] = \frac{1}{\mu(1 - \rho)} = \frac{1}{\mu - \lambda}, \quad (22)$$

where μ is the service rate and $\rho = \frac{\lambda}{\mu}$ is the server utilization ratio.

To calculate the upper bound for the M/M/1 system, we consider

$$\begin{aligned} E[Y^2] &= \int_0^\infty y^2 \lambda e^{-\lambda y} dy \\ &= \lambda e^{-\lambda y} \left(-\frac{y^2}{\lambda} - \frac{2y}{\lambda^2} - \frac{2}{\lambda^3} \right) \Big|_0^\infty \end{aligned} \quad (23)$$

$$= \frac{2}{\lambda^2}, \quad (24)$$

where (23) follows according to [30, Eq. (2.322.2)].

By substituting (20), (22) and (24) into (15), we have

$$\Delta_{(k)}^{\text{UB}} = \frac{1}{\mu - \lambda} + \frac{2/\lambda^2}{2/\lambda} + \frac{k/\lambda}{2} = \frac{1}{\mu - \lambda} + \frac{1}{\lambda} + \frac{k}{2\lambda}, \quad (25)$$

which can be further substituted into (11) to upper bound the average AoI for the system with outage events as

$$\Delta^{\text{UB}} = (1 - P_{\text{out}})^2 \sum_{k=0}^{\infty} P_{\text{out}}^k (k+1) \Delta_{(k)}^{\text{UB}} \quad (26)$$

$$= (1 - P_{\text{out}})^2 \sum_{k=0}^{\infty} P_{\text{out}}^k (k+1) \left(\frac{1}{\mu - \lambda} + \frac{1}{\lambda} + \frac{k}{2\lambda} \right)$$

$$= (1 - P_{\text{out}})^2 \sum_{k=0}^{\infty} P_{\text{out}}^k (k+1) \left(\frac{1}{\mu - \lambda} + \frac{1}{\lambda} \right)$$

$$+ (1 - P_{\text{out}})^2 \sum_{k=0}^{\infty} P_{\text{out}}^k (k+1) \frac{k}{2\lambda}$$

$$= \frac{1}{\mu - \lambda} + \frac{1}{\lambda} + \frac{(1 - P_{\text{out}})^2}{2\lambda} \sum_{k=0}^{\infty} P_{\text{out}}^k k(k+1), \quad (27)$$

where (27) follows according to [30, Eq. (0.231.2)] for $P_{\text{out}} < 1$.

In order to calculate $\sum_{k=0}^{\infty} P_{\text{out}}^k k(k+1)$, let $\zeta = \sum_{k=0}^{\infty} P_{\text{out}}^k \cdot k(k+1)$ and consider

$$\zeta P_{\text{out}} = \sum_{k=0}^{\infty} P_{\text{out}}^{k+1} k(k+1) = \sum_{k=1}^{\infty} P_{\text{out}}^k (k-1)k. \quad (28)$$

Then, we have

$$\begin{aligned} \zeta(1 - P_{\text{out}}) &= \zeta - \zeta P_{\text{out}} \\ &= \sum_{k=0}^{\infty} P_{\text{out}}^k k(k+1) - \sum_{k=1}^{\infty} P_{\text{out}}^k (k-1)k \\ &= \sum_{k=1}^{\infty} P_{\text{out}}^k [k(k+1) - (k-1)k] \\ &= \sum_{k=1}^{\infty} 2k P_{\text{out}}^k \\ &= \frac{2P_{\text{out}}}{(1 - P_{\text{out}})^2}, \end{aligned} \quad (29)$$

where (29) follows according to [30, Eq. (0.231.2)] for $P_{\text{out}} < 1$. Hence, we can obtain

$$\sum_{k=0}^{\infty} P_{\text{out}}^k k(k+1) = \zeta = \frac{2P_{\text{out}}}{(1 - P_{\text{out}})^3}. \quad (30)$$

By substituting (30) into (27), we can obtain the closed-form expression of the upper bound as

$$\begin{aligned} \Delta^{\text{UB}} &= \frac{1}{\mu - \lambda} + \frac{1}{\lambda} + \frac{(1 - P_{\text{out}})^2}{2\lambda} \cdot \frac{2P_{\text{out}}}{(1 - P_{\text{out}})^3} \\ &= \frac{1}{\mu - \lambda} + \frac{1}{\lambda} + \frac{P_{\text{out}}}{\lambda(1 - P_{\text{out}})} \\ &= \frac{1}{\mu - \lambda} + \frac{1}{\lambda(1 - P_{\text{out}})}. \end{aligned} \quad (31)$$

Remark: Δ^{UB} is an increasing function of P_{out} . This matches our intuition that the average AoI increases as P_{out} goes larger.

B. Relative Error and Refined Upper Bound

The relative error between the upper bound and the exact value of the average AoI is defined by

$$err = \frac{\Delta^{UB} - \Delta}{\Delta}. \quad (32)$$

When $k = 0$, the exact value of the average AoI $\Delta_{(0)}$ is given by [28, Eq. (2.19)]

$$\Delta_{(0)} = \frac{1}{\mu} \left(1 + \frac{1}{\rho} + \frac{\rho^2}{1-\rho} \right). \quad (33)$$

Therefore, we can calculate the relative error between the upper bound and the exact value of the average AoI for $k = 0$ as

$$\begin{aligned} err_{(0)} &= \frac{\Delta_{(0)}^{UB} - \Delta_{(0)}}{\Delta_{(0)}} \\ &= \frac{\left[\frac{1}{\mu-\lambda} + \frac{1}{\lambda} + \frac{0}{2\lambda} - \frac{1}{\mu} \left(1 + \frac{1}{\rho} + \frac{\rho^2}{1-\rho} \right) \right]}{\left[\frac{1}{\mu} \left(1 + \frac{1}{\rho} + \frac{\rho^2}{1-\rho} \right) \right]} \\ &= \frac{1}{1 - \rho^2 + \rho^3} - 1. \end{aligned} \quad (34)$$

Notice that when $P_{out} = 0$, the average AoI for the system with outage events in (11) reduces to the average AoI without outage events. Hence, (34) is the relative error of the upper bound on the average AoI for reliable communications. For $k > 0$, since the exact expression of the average AoI is still an open problem, we need to utilize numerical results to evaluate the relative error of the upper bound.

Since we already know the exact expression of the average AoI for $k = 0$, we can replace $\Delta_{(0)}^{UB}$ with $\Delta_{(0)}$ to reduce the relative error when calculating the upper bound from (26). Then, the refined upper bound is obtained from (11) as

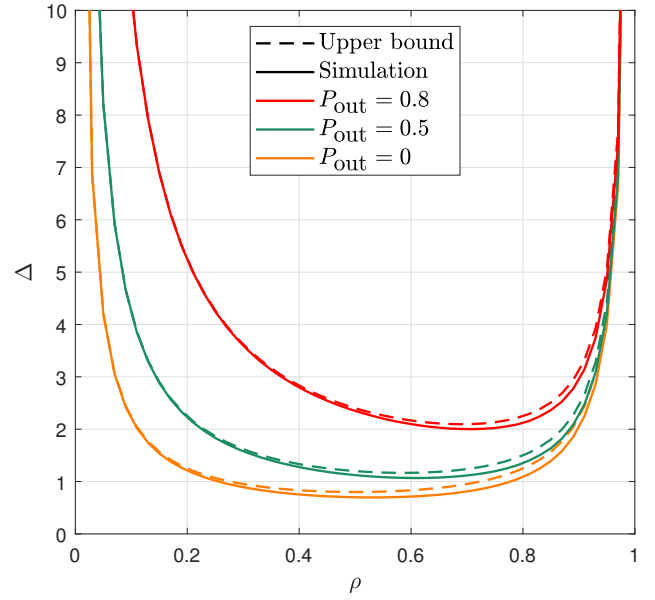
$$\begin{aligned} \Delta^{UB*} &= (1 - P_{out})^2 \left[\sum_{k=0}^{\infty} P_{out}^k (k+1) \Delta_{(k)}^{UB} - \Delta_{(0)}^{UB} + \Delta_{(0)} \right] \\ &= \Delta^{UB} + (1 - P_{out})^2 \left[-\Delta_{(0)}^{UB} + \Delta_{(0)} \right] \end{aligned} \quad (35)$$

$$\begin{aligned} &= \frac{1}{\mu - \lambda} + \frac{1}{\lambda(1 - P_{out})} + (1 - P_{out})^2 \\ &\quad \cdot \left[-\frac{1}{\mu - \lambda} - \frac{1}{\lambda} + \frac{1}{\mu} \left(1 + \frac{1}{\rho} + \frac{\rho^2}{1-\rho} \right) \right] \\ &= \frac{1}{\mu - \lambda} + \frac{1}{\lambda(1 - P_{out})} - \frac{\lambda(1 - P_{out})^2}{\mu^2}. \end{aligned} \quad (36)$$

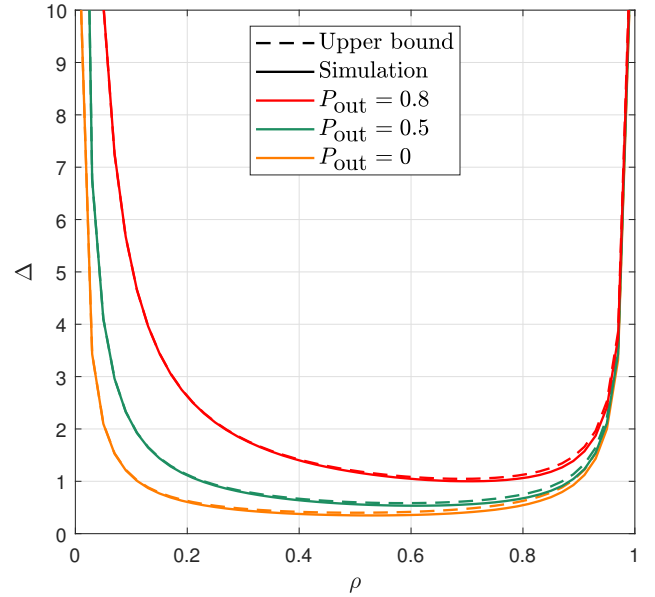
C. Numerical Results

1) *Upper Bound*: We evaluate the exact average AoI for the system with outage events by Monte Carlo simulation [31]. Fig. 4 compares the upper bound with the simulation results with respect to the average AoI. It is noticeable that the gap between the upper bound and the exact average AoI becomes smaller as the service rate μ increases. Interestingly, the gap seems not sensitive to the outage probability, i.e., the deviation degrees are similar even though P_{out} varies within a large range from 0 to 0.8.

Fig. 5 illustrates the curves of the refined upper bound. It is certain that the refined upper bound for $P_{out} = 0$ should



(a) $\mu = 5$.



(b) $\mu = 10$.

Fig. 4. Upper bound on the average AoI.

coincide with the exact average AoI without outage events. However, the improvement of the refined upper bound is not obvious for a large outage probability, because (35) indicates that the weight of $\Delta_{(0)}$ reduces as P_{out} increases. Therefore, the effect of refinement by replacing $\Delta_{(0)}^{UB}$ with $\Delta_{(0)}$ also decreases if the outage probability becomes larger.

2) *Relative Error*: As shown in Fig. 6, the relative errors of the upper bound and the refined upper bound are relatively small, and represent the tightness of the upper bound. Moreover, Fig. 6(a) demonstrates that the relative error decreases as the outage probability increases. This observation matches the phenomenon in Fig. 4 that the deviation degrees are similar for diverse P_{out} , and hence the relative error decreases when the

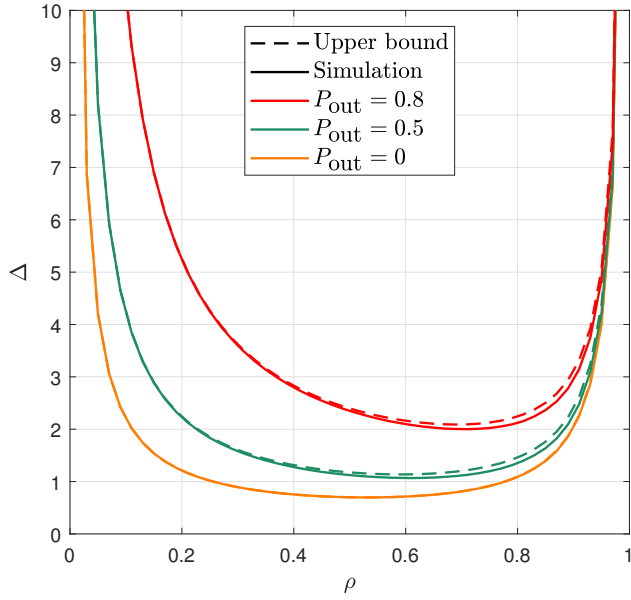
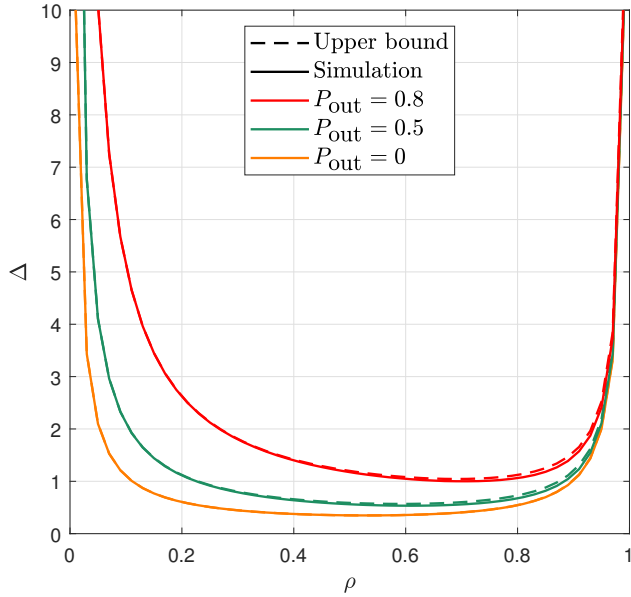
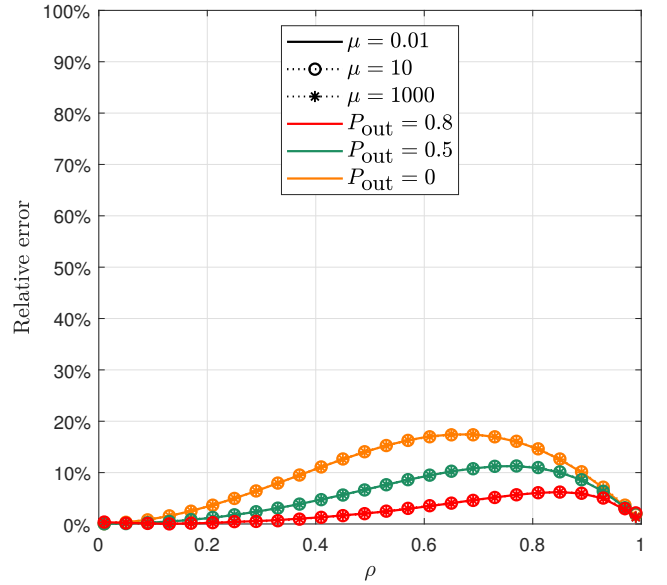
(a) $\mu = 5$.(b) $\mu = 10$.

Fig. 5. Refined upper bound on the average AoI.

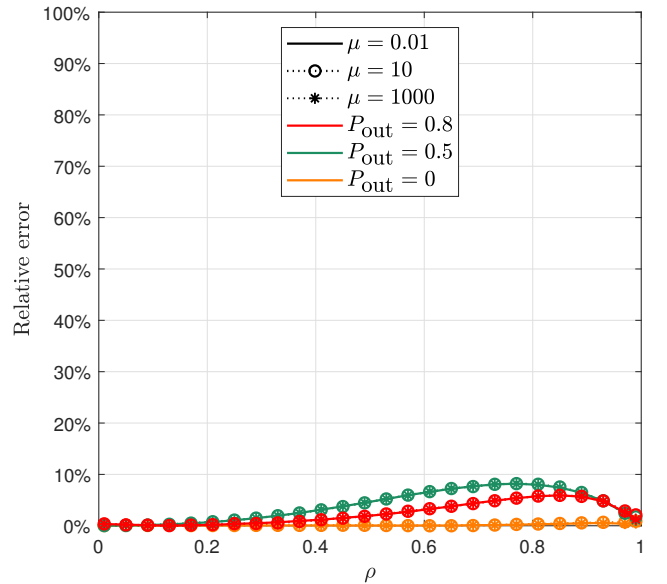
average AoI increases for larger P_{out} . Interestingly, the curves completely coincide with each other for different μ , even if μ is scaled by a huge degree, e.g., from 0.01 to 1000. This observation implies that the relative error is a function of ρ and P_{out} as denoted by $\text{err}(\rho, P_{\text{out}})$.

IV. AOI OPTIMIZATION

In this section, we optimize the average AoI based on the upper bound for a system with energy limitation. For simplicity, we consider a basic point-to-point lossy communication model with only one Gaussian source and one destination. Initially, the communication model is introduced in detail in Section IV-A. Then, Section IV-B derives a closed-form



(a) Upper bound.



(b) Refined upper bound.

Fig. 6. Relative error of the upper bound.

expression of the outage probability. In Section IV-C, we prove the convexity of the refined upper bound and utilize it for solving the optimal trade-off among the parameters related to the average AoI. The numerical results of AoI optimization are provided in Section IV-D.

A. Communication Model

1) *System Model*: The M/M/1 system with the FCFS scheme has an i.i.d. Gaussian source $X \sim N(0, \sigma^2)$ generating information updates in the form of Gaussian sequences at the mean rate λ . In practical systems, the source could be a sensor, and hence we can control the generating rate λ of updates. This fundamental assumption allows us to optimize the average AoI by adjusting λ . The update sequences are encoded, and then

continuously transmitted to a destination having a buffer with a sufficiently large size. Then, the destination processes the received update sequences at the mean service rate μ . After decoding, the distortion of the reconstructed update sequence is evaluated, Gaussian symbol by symbol, by quadratic (squared error) distortion measure $d_Q(x, \hat{x}) = (x - \hat{x})^2$. If the average distortion of a reconstructed update sequence is larger than the specified distortion requirement D , the reconstructed update sequence is discarded and an outage event occur.

2) *Channel Model*: The transmissions are assumed to suffer from independent block Rayleigh fading. For a transmitted symbol x_t with transmission power $P_t = \mathbb{E}[|x_t|^2]$, the received symbol x_r is expressed by

$$x_r = \sqrt{G}hx_t + z, \quad (37)$$

where G is the geometric gain dominated by the environment conditions and the locations of the source and the destination. h represents the complex channel gain which is normalized to unity or $\mathbb{E}[|h|^2] = 1$ for simplicity. z stands for the zero-mean additive white Gaussian noise (AWGN) with its power spectral density being N_0 . Then, the instantaneous signal-to-noise ratio (SNR) and the average SNR are given by

$$\gamma = \frac{G|h|^2 P_t}{N_0}, \quad (38)$$

$$\bar{\gamma} = \frac{G P_t}{N_0}. \quad (39)$$

Obviously, $|h|^2 = \frac{\gamma}{G}$, and hence the PDF of the instantaneous SNR for Rayleigh fading is

$$f_{\text{SNR}}(\gamma) = \frac{1}{\bar{\gamma}} \exp\left(-\frac{\gamma}{\bar{\gamma}}\right). \quad (40)$$

B. Outage Probability

To derive the outage probability, we need to determine the condition when the distortion requirement can be satisfied. According to [32, Theorem 10.3.2], the rate-distortion function of a Gaussian source $X \sim N(0, \sigma^2)$ for the distortion degree D is given by

$$R(D) = \frac{1}{2} \log^+ \left(\frac{\sigma^2}{D} \right), \quad (41)$$

where $\log^+(\cdot) = \max\{\log(\cdot), 0\}$, and the base of logarithm function $\log(\cdot)$ is assumed to be 2 unless specified. Then, the Shannon's lossy source-channel separation theorem indicates that the distortions D can be satisfied if [33, Theorem 3.7]

$$rR(D) \leq C(\gamma), \quad (42)$$

where r stands for the end-to-end rate of joint source-channel coding, and $C(\gamma) = \log(1+\gamma)$ is the Shannon capacity for two dimensional signaling using Gaussian codebook. Let $c = C(\gamma)$ be the instantaneous channel capacity, and then we have

$$\gamma = 2^c - 1. \quad (43)$$

Based on the concept of transformation of random variables [29, Chapter 5], the characteristic function of c is given by [29, Eq. (5-114)]

$$\Phi_C(\omega) = \int_{-\infty}^{\infty} \exp(j\omega C(\gamma)) \cdot f_{\text{SNR}}(\gamma) d\gamma$$

$$\begin{aligned} &= \int_{-\infty}^{\infty} \exp(j\omega c) \cdot \frac{1}{\bar{\gamma}} \exp\left(-\frac{2^c - 1}{\bar{\gamma}}\right) d(2^c - 1) \\ &= \int_{-\infty}^{\infty} \exp(j\omega c) \cdot \frac{2^c \ln 2}{\bar{\gamma}} \exp\left(-\frac{2^c - 1}{\bar{\gamma}}\right) dc. \end{aligned} \quad (44)$$

Hence, the PDF of the instantaneous channel capacity is

$$f_C(c) = \frac{2^c \ln 2}{\bar{\gamma}} \exp\left(-\frac{2^c - 1}{\bar{\gamma}}\right). \quad (45)$$

Consequently, given a distortion requirement D , the outage probability can be calculated by the probability that the instantaneous channel capacity is less than $rR(D)$, i.e.,

$$\begin{aligned} P_{\text{out}} &= \int_0^{rR(D)} f_C(c) dc \\ &= \int_0^{rR(D)} \frac{2^c \ln 2}{\bar{\gamma}} \exp\left(-\frac{2^c - 1}{\bar{\gamma}}\right) dc \\ &= -\exp\left(-\frac{2^c - 1}{\bar{\gamma}}\right) \Big|_0^{rR(D)} \\ &= 1 - \exp\left(-\frac{2^{rR(D)} - 1}{\bar{\gamma}}\right) \\ &= 1 - \exp\left(-\frac{\text{pow}\left[2, \frac{r}{2} \log^+ \left(\frac{\sigma^2}{D}\right)\right] - 1}{\bar{\gamma}}\right) \\ &= 1 - \exp\left(-\frac{\left[(\sigma^2/D)^{\frac{r}{2}} - 1\right]^+}{\bar{\gamma}}\right), \end{aligned} \quad (46)$$

where $\text{pow}(a, b) = a^b$.

C. AoI Minimization

Assuming that P_T is the total transmission energy in a unit of time, then P_T/λ is the transmission power of each update for mean arrival rate being λ^1 . Therefore, the average SNR is

$$\bar{\gamma} = \frac{G P_T}{\lambda N_0}. \quad (47)$$

Then, we have

$$\begin{aligned} \Delta^{\text{UB}*} &= \frac{1}{\mu - \lambda} + \frac{1}{\lambda} \exp\left(-\frac{\left[(\sigma^2/D)^{\frac{r}{2}} - 1\right]^+}{\bar{\gamma}}\right) - \frac{\lambda}{\mu^2} \\ &\quad \cdot \exp\left(-\frac{2 \left[(\sigma^2/D)^{\frac{r}{2}} - 1\right]^+}{\bar{\gamma}}\right) \\ &= \frac{1}{\mu - \lambda} + \frac{1}{\lambda} \exp\left(-\frac{\lambda N_0 \left[(\sigma^2/D)^{\frac{r}{2}} - 1\right]^+}{G P_T}\right) \\ &\quad - \frac{\lambda}{\mu^2} \exp\left(-\frac{2\lambda N_0 \left[(\sigma^2/D)^{\frac{r}{2}} - 1\right]^+}{G P_T}\right) \end{aligned}$$

¹Notice that the transmission power of each update increases as λ decreases, and P_T/λ goes extremely large if λ tends to 0. However, practical systems may not support such a large transmission power. This limitation on the maximum transmission power can be considered as a constraint for AoI optimization in practical systems.

$$= \frac{1}{\mu - \lambda} + \frac{1}{\lambda} e^{\xi\lambda} - \frac{\lambda}{\mu^2} e^{-2\xi\lambda}, \quad (48)$$

where we define $\xi = \frac{N_0[(\sigma^2/D)^{\frac{r}{2}} - 1]^+}{GP_T}$ for conciseness.

Now, we prove the convexity of $\Delta^{\text{UB}*}$ below. Consider

$$\begin{aligned} \frac{\partial^2 \Delta^{\text{UB}*}}{\partial \lambda^2} &= \frac{2}{(\mu - \lambda)^3} + \frac{e^{\xi\lambda}}{\lambda^3} (\xi^2 \lambda^2 - 2\xi\lambda + 2) \\ &\quad - \frac{4\xi e^{-2\xi\lambda}}{\mu^2} (\xi\lambda - 1) \\ &= \frac{2}{(\mu - \lambda)^3} + \frac{e^{\xi\lambda}}{\lambda^3} [(\xi\lambda - 1)^2 + 1] \\ &\quad - \frac{4\xi e^{-2\xi\lambda}}{\mu^2} (\xi\lambda - 1). \end{aligned} \quad (49)$$

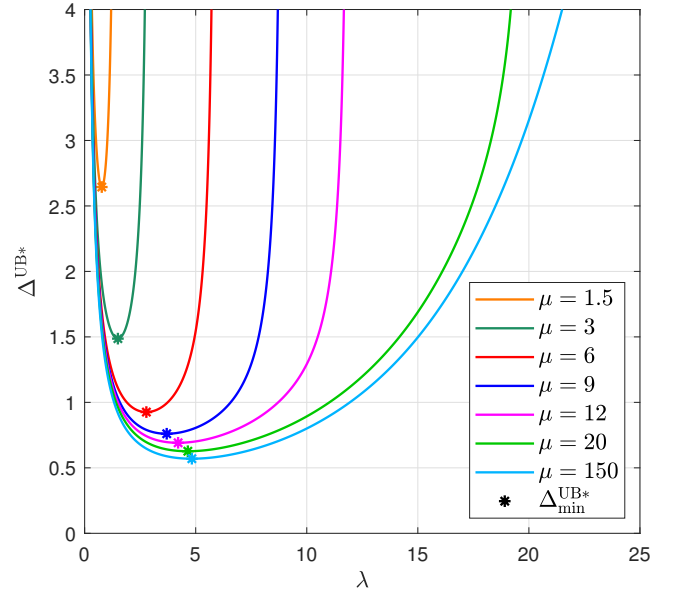
When $\xi\lambda - 1 \leq 0$, it is obvious that $\frac{\partial^2 \Delta^{\text{UB}*}}{\partial \lambda^2} > 0$ since $\mu > \lambda > 0$. When $\xi\lambda - 1 > 0$, we have $e^{\xi\lambda} > e$ and $e^{\xi\lambda} > \xi\lambda$. Then, consider

$$\begin{aligned} &\frac{e^{\xi\lambda}}{\lambda^3} [(\xi\lambda - 1)^2 + 1] \\ &= \frac{e^{\xi\lambda} \cdot e^{2\xi\lambda} \cdot e^{-2\xi\lambda}}{\lambda \cdot \lambda^2} [(\xi\lambda - 1)^2 + 1] \\ &> \frac{\xi\lambda \cdot e^2 \cdot e^{-2\xi\lambda}}{\lambda \cdot \mu^2} [(\xi\lambda - 1)^2 + 1] \\ &= \frac{\xi e^2 \cdot e^{-2\xi\lambda}}{\mu^2} [\xi^2 \lambda^2 - 3\xi\lambda + 3 + (\xi\lambda - 1)] \\ &= \frac{\xi e^2 \cdot e^{-2\xi\lambda}}{\mu^2} \left[\left(\xi\lambda - \frac{3}{2} \right)^2 + \frac{3}{4} + (\xi\lambda - 1) \right] \\ &> \frac{4\xi e^{-2\xi\lambda}}{\mu^2} (\xi\lambda - 1). \end{aligned} \quad (50)$$

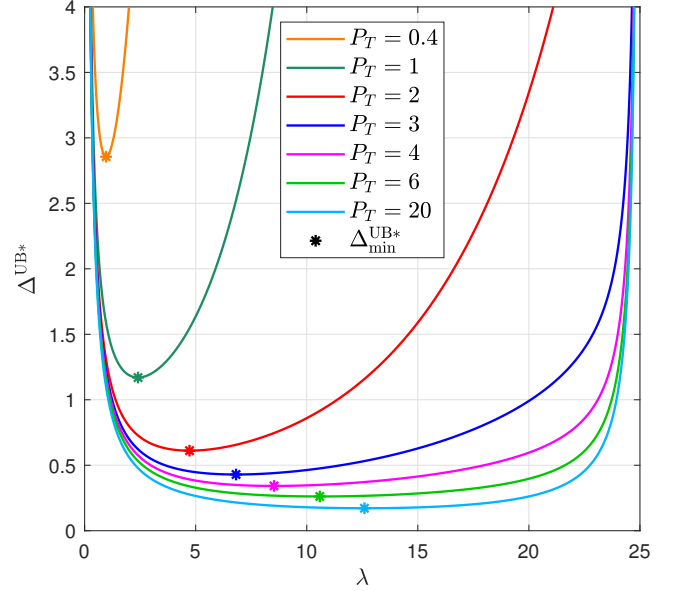
By substituting (50) into (49), we can obtain $\frac{\partial^2 \Delta^{\text{UB}*}}{\partial \lambda^2} > 0$. Consequently, $\Delta^{\text{UB}*}$ is a convex function with respect to λ , and we can minimize $\Delta^{\text{UB}*}$ by convex optimization.

D. Numerical Results

Fig. 7(a) and Fig. 7(b) illustrate the tendency of $\Delta^{\text{UB}*}$ for diverse values of μ and P_T , respectively. Certainly, the average AoI and the minimum average AoI decrease as μ or P_T increases. Nevertheless, the performance gain also decreases fast as μ or P_T increases, especially when $\mu \geq 20$ and $P_T \geq 6$. This is because larger μ allows λ to be larger to reduce the maximum AoI of each transmission. However, since the P_T is fixed in Fig. 7(a), larger λ reduces the transmission power resulting in a higher outage probability. When the transmission power decreases to a relatively small value, the outage probability becomes the dominant factor of the average AoI. Hence, it is difficult to further increase λ , and even larger μ can hardly affect the average AoI. For Fig. 7(b), larger P_T allows λ to increase for reducing the maximum AoI, while keeping the outage probability at a relatively low level. However, the optimal λ is constrained by fixed μ , i.e., λ cannot increase arbitrarily. Therefore, when P_T is sufficiently large, the outage probability already remains extremely low and it is difficult to obtain more gains. Another phenomenon is that when P_T becomes sufficiently large, the outage probability



(a) $P_T = 2$.



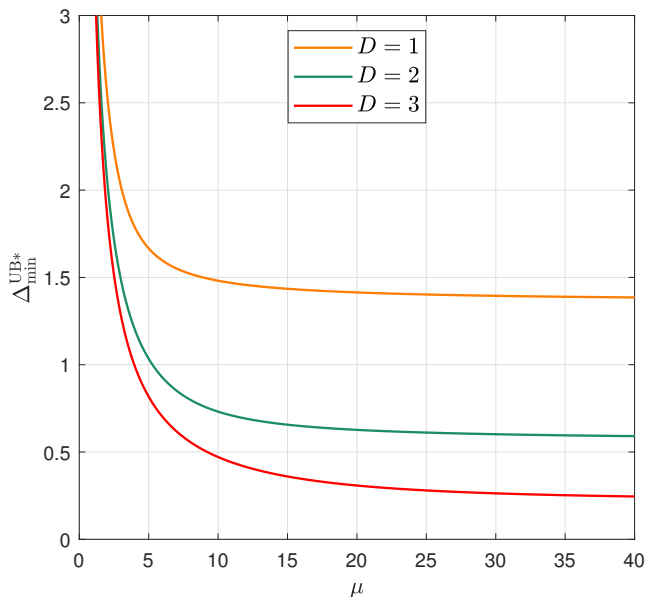
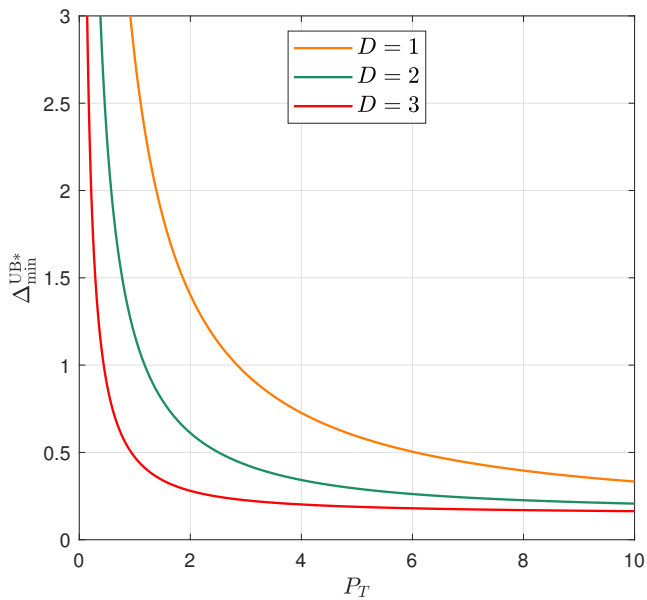
(b) $\mu = 25$.

Fig. 7. $\Delta^{\text{UB}*}$ for $\sigma = 2, D = 2, N_0 = 1, G = 1$ and $r = 1$.

keeps at almost 0 in spite of λ , and hence the curve of the average AoI has the same shape as the curve without outage events.

Fig. 8 depicts minimum $\Delta^{\text{UB}*}$ for various distortion requirements. Clearly, the minimum average AoI decreases as the distortion requirement D increases, because the outage probability is lower for less strict distortion requirements. Fig. 8(a) and Fig. 8(b) show that the minimum average AoI decreases slowly as μ and P_T become relatively large, respectively. This observation matches the result in Fig. 7 as discussed above.

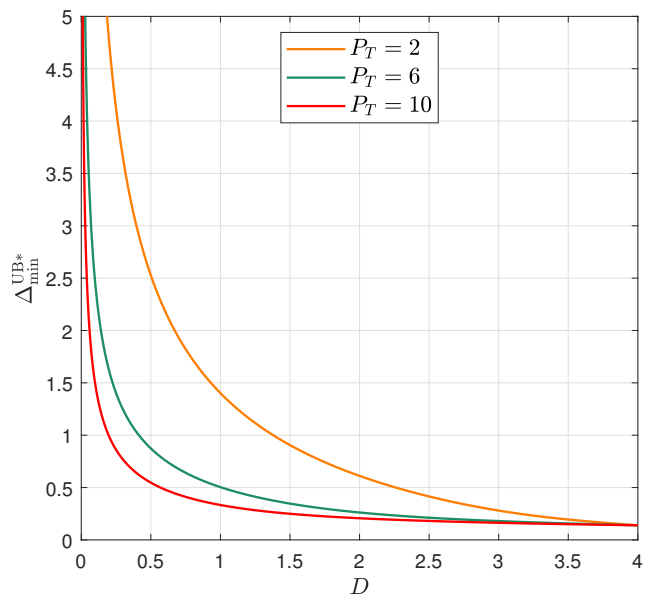
It is found from Fig. 9 that the minimum average AoI decreases rapidly when D is small. This can be understood

(a) $P_T = 2$.(b) $\mu = 25$.Fig. 8. Minimum $\Delta^{\text{UB}*}$ for $\sigma = 2, N_0 = 1, G = 1$ and $r = 1$.

from the rate-distortion function that small D requires an extremely high rate, resulting in a very large outage probability. Moreover, the minimum average AoI finally converges together when $D = \sigma^2 = 4$. This is because $D \geq \sigma^2$ can be always satisfied with the Gaussian source at the zero source coding rate, which means that the outage event will never occur regardless of P_T .

V. CONCLUSION

In this paper, we have established an analytical framework of the upper bound on the average AoI in outage-acceptable G/G/1 systems with the FCFS scheme. We, first of all, characterized a general upper bound on the average

Fig. 9. Minimum $\Delta^{\text{UB}*}$ for $\sigma = 2, N_0 = 1, G = 1, r = 1$ and $\mu = 25$.

AoI for a specified outage probability. Then, we conducted the AoI analysis for the M/M/1 system, and we obtained a concise closed-form expression of the upper bound on the average AoI. We also evaluated the relative error of the upper bound, and further proposed a refined upper bound on the average AoI. Furthermore, we derived a closed-form expression of the outage probability for point-to-point lossy communications with a Gaussian source suffering from block Rayleigh fading. We proved the convexity of the refined upper bound on the average AoI with respect to the generating rate of updates. With the convex optimization framework based on the refined upper bound, we identified the trade-off between the generating rate of updates and the transmission power for minimizing the average AoI. The numerical results indicate that if either μ or P_T is fixed, the performance gain in terms of the reduction of minimum average AoI is extremely small even when the unfixed parameter becomes large.

APPENDIX A CALCULATIONS FOR (8)-(10)

$$\begin{aligned}
 \mathbb{E}[\tilde{Y}\tilde{T}] &= \mathbb{E}[\tilde{Y}_i\tilde{T}_i] \\
 &= \mathbb{E}\left[\left(\sum_{j=i}^{i+k} Y_j\right) \cdot T_{i+k}\right] \\
 &= \sum_{j=i}^{i+k} \mathbb{E}[Y_j T_{i+k}] \\
 &= \sum_{j=i}^{i+k} \mathbb{E}[Y_j(W_{i+k} + S_{i+k})] \\
 &= \sum_{j=i}^{i+k} \mathbb{E}[Y_j W_{i+k}] + \sum_{j=i}^{i+k} \mathbb{E}[Y_j S_{i+k}]
 \end{aligned}$$

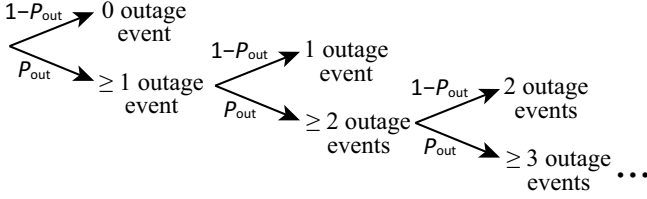


Fig. 10. The probability of k successive outage events.

$$= \sum_{j=i}^{i+k} E[Y_j W_{i+k}] + (k+1)E[Y]E[S]. \quad (51)$$

$$\begin{aligned} E[\tilde{Y}^2] &= E[\tilde{Y}_i^2] \\ &= E\left[\left(\sum_{j=i}^{i+k} Y_j\right)^2\right] \\ &= E\left[\sum_{j=i}^{i+k} Y_j^2 + 2 \sum_{j=i}^{i+k-1} \sum_{j'=j+1}^{i+k} Y_j Y_{j'}\right] \\ &= (k+1)E[Y^2] + 2 \sum_{j=i}^{i+k-1} \sum_{j'=j+1}^{i+k} E[Y_j]E[Y_{j'}] \\ &= (k+1)E[Y^2] + k(k+1)(E[Y])^2 \\ &= (k+1)(E[Y^2] + k(E[Y])^2). \end{aligned} \quad (52)$$

$$E[\tilde{Y}] = E[\tilde{Y}_i] = E\left[\sum_{j=i}^{i+k} Y_j\right] = \sum_{j=i}^{i+k} E[Y_j] = (k+1)E[Y]. \quad (53)$$

APPENDIX B PROOF OF PROPOSITION 1

To derive the average AoI for the system in the stable states, we need to take the probability of the outage events successively occurring k times into account. As illustrated in Fig. 10, given an outage probability P_{out} , the probability of no outage event is $(1 - P_{\text{out}})$, and hence $(1 - P_{\text{out}})$ corresponds to the event space without outage event. The remaining event space P_{out} corresponds to one or more than one outage events. Then, we can further divide the event space of $k \geq 1$ into the event spaces of $k = 1$ and of $k \geq 2$ with the probabilities being $(1 - P_{\text{out}})$ and P_{out} , respectively. By recursively dividing the event spaces, we can obtain the probability of successively occurring k outage events as $P_{\text{out}}^k (1 - P_{\text{out}})$. For a sufficiently large N_T of successful transmissions, the number of k successive outage events is $N_T \cdot P_{\text{out}}^k (1 - P_{\text{out}})$. Furthermore, the average area of trapezoids with k outage events is

$$\begin{aligned} E[\tilde{Q}] &= \Delta_{(k)} E[\tilde{Y}] \\ &= \Delta_{(k)} E\left[\sum_{j=i}^{i+k} Y_j\right] \\ &= \Delta_{(k)} \sum_{j=i}^{i+k} E[Y_j] \end{aligned}$$

$$= \Delta_{(k)} (k+1) E[Y]. \quad (54)$$

Therefore, the summation of all \tilde{Q}_i for k successive outage events in N_T successful transmissions is $N_T P_{\text{out}}^k (1 - P_{\text{out}}) \cdot \Delta_{(k)} (k+1) E[Y]$. Hence, the total area under $\Delta(t)$ in N_T successful transmissions is given by $\sum_{k=0}^{\infty} N_T P_{\text{out}}^k (1 - P_{\text{out}}) \cdot \Delta_{(k)} (k+1) E[Y]$. Likewise, we can obtain the total time for N_T successful transmissions as $\sum_{k=0}^{\infty} N_T P_{\text{out}}^k (1 - P_{\text{out}}) \cdot (k+1) E[Y]$. Consequently, the average AoI for the system with outage events is

$$\begin{aligned} \Delta &= \frac{\sum_{k=0}^{\infty} N_T P_{\text{out}}^k (1 - P_{\text{out}}) \cdot \Delta_{(k)} (k+1) E[Y]}{\sum_{k=0}^{\infty} N_T P_{\text{out}}^k (1 - P_{\text{out}}) \cdot (k+1) E[Y]} \\ &= \frac{\sum_{k=0}^{\infty} P_{\text{out}}^k (k+1) \Delta_{(k)}}{\sum_{k=0}^{\infty} P_{\text{out}}^k (k+1)} \\ &= \frac{\sum_{k=0}^{\infty} P_{\text{out}}^k (k+1) \Delta_{(k)}}{1/(1 - P_{\text{out}})^2} \end{aligned} \quad (55)$$

$$= (1 - P_{\text{out}})^2 \sum_{k=0}^{\infty} P_{\text{out}}^k (k+1) \Delta_{(k)}, \quad (56)$$

where (55) follows according to [30, Eq. (0.231.2)] for $P_{\text{out}} < 1$. Obviously, when $P_{\text{out}} = 1$, the transmission always fails and hence the average AoI becomes ∞ .

This finishes the proof of *Proposition 1*.

APPENDIX C PROOF OF PROPOSITION 2

Consider

$$\begin{aligned} E[Y] &= \int_0^{\infty} y f_Y(y) dy \\ &= \int_0^{\infty} y \int_0^{\infty} f_{Y|W}(y|w) f_W(w) dw dy \\ &= \int_0^{\infty} f_W(w) dw \int_0^{\infty} y f_{Y|W}(y|w) dy \\ &= \int_0^{\infty} f_W(w) E[Y|W = w] dw. \end{aligned} \quad (57)$$

Therefore, we have

$$\begin{aligned} E[Y_j] &= \int_0^{\infty} f_{W_{i-1}}(w) E[Y_j | W_{i-1} = w] dw \\ &= \int_0^{\infty} f_{W_{i+k}}(w) E[Y_j | W_{i+k} = w] dw. \end{aligned} \quad (58)$$

On the one hand, W_{i-1} is independent of Y_j , i.e., $E[Y_j | W_{i-1} = w] = E[Y_j]$, because $i-1 < j$. On the other hand, if Y_j is larger, it means that the j -th packet arrives later, and recursively the $(i+k)$ -th packet also arrives later. Hence, the system has more time to serve the packets in the queue, and the waiting time W_{i+k} becomes smaller. Consequently, the smaller W_{i+k} , the larger $E[Y_j | W_{i+k} = w]$, i.e.,

$$E[Y_j | W_{i+k} = w] < E[Y_j | W_{i+k} = w'], \quad \text{for any } w > w'. \quad (59)$$

Obviously, $E[Y_j | W_{i+k} = w]$ is a monotonically decreasing function with respect to w . Moreover, $E[Y_j | W_{i+k} = w]$ must have some values larger than $E[Y_j]$ and some other values smaller than $E[Y_j]$. Otherwise, let us assume that

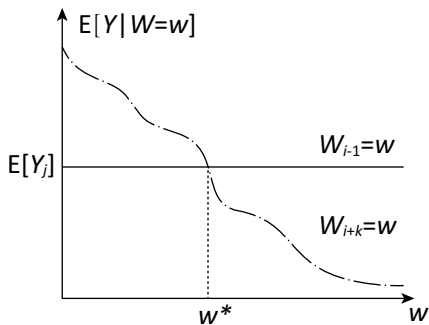


Fig. 11. The tendencies of $E[Y_j|W_{i-1} = w]$ and $E[Y_j|W_{i+k} = w]$.

$E[Y_j] \geq E[Y_j|W_{i+k} = w]$ always holds. Since $f_{W_{i-1}}(w) = f_{W_{i+k}}(w) = f_W(w) \geq 0$, we have

$$\begin{aligned} f_{W_{i-1}}(w)E[Y_j|W_{i-1} = w] \\ \geq f_{W_{i+k}}(w)E[Y_j|W_{i+k} = w] \end{aligned} \quad (60)$$

$$\begin{aligned} \int_0^\infty f_{W_{i-1}}(w)E[Y_j|W_{i-1} = w]dw \\ > \int_0^\infty f_{W_{i+k}}(w)E[Y_j|W_{i+k} = w]dw, \end{aligned} \quad (61)$$

where the equality of (61) cannot hold because $E[Y_j|W_{i+k} = w]$ is monotonically decreasing. Clearly, (61) conflicts with (58), and hence the assumption that $E[Y_j] \geq E[Y_j|W_{i+k} = w]$ for all w is incorrect. Similarly, we can also prove that $E[Y_j] \leq E[Y_j|W_{i+k} = w]$ cannot always hold. Consequently, the tendencies of $E[Y_j|W_{i+k} = w]$ and $E[Y_j|W_{i-1} = w]$ are like the curves illustrated in Fig. 11, where the convexity or concavity of $E[Y_j|W_{i+k} = w]$ does not matter.

In addition, due to the monotonicity of $E[Y_j|W_{i+k} = w]$, the two curves must have one and only one cross point $(w^*, E[Y_j])$, and

$$E[Y_j|W_{i+k} = w] > E[Y_j|W_{i-1} = w], \quad \text{for } 0 \leq w < w^*, \quad (62)$$

$$E[Y_j|W_{i+k} = w] < E[Y_j|W_{i-1} = w], \quad \text{for } w > w^*. \quad (63)$$

Furthermore, since $f_{W_{i-1}}(w) = f_{W_{i+k}}(w) = f_W(w) \geq 0$, we have

$$\begin{aligned} f_{W_{i+k}}(w)E[Y_j|W_{i+k} = w] > f_{W_{i-1}}(w)E[Y_j|W_{i-1} = w], \\ \text{for } 0 \leq w < w^*, \end{aligned} \quad (64)$$

$$\begin{aligned} f_{W_{i+k}}(w)E[Y_j|W_{i+k} = w] < f_{W_{i-1}}(w)E[Y_j|W_{i-1} = w], \\ \text{for } w > w^*. \end{aligned} \quad (65)$$

Now, we introduce the following lemma to bound $E[Y_j|W_{i+k}]$.

Lemma 1 (integral scaling lemma): If two functions $g_1(w)$ and $g_2(w)$ satisfy

$$\int_0^\infty g_1(w)dw = \int_0^\infty g_2(w)dw, \quad (66)$$

$$g_2(w) > g_1(w), \quad \text{for } 0 \leq w < w^*, \quad (67)$$

$$g_2(w) < g_1(w), \quad \text{for } w > w^*, \quad (68)$$

then the following inequality holds

$$\int_0^\infty w g_2(w)dw < \int_0^\infty w g_1(w)dw. \quad (69)$$

The proof of Lemma 1 is presented in Appendix D. Let $g_1(w) = f_{W_{i-1}}(w)E[Y_j|W_{i-1} = w]$ and $g_2(w) = f_{W_{i+k}}(w)E[Y_j|W_{i+k} = w]$, and hence we have

$$\begin{aligned} \int_0^\infty w f_{W_{i+k}}(w)E[Y_j|W_{i+k} = w]dw \\ < \int_0^\infty w f_{W_{i-1}}(w)E[Y_j|W_{i-1} = w]dw. \end{aligned} \quad (70)$$

Moreover, consider

$$\begin{aligned} E[YW] &= \int_0^\infty \int_0^\infty y w f_{Y,W}(y, w) dy dw \\ &= \int_0^\infty \int_0^\infty y w f_{Y|W}(y|w) f_W(w) dy dw \\ &= \int_0^\infty w f_W(w) dw \int_0^\infty y f_{Y|W}(y|w) dy \\ &= \int_0^\infty w f_W(w) E[Y|W = w] dw. \end{aligned} \quad (71)$$

By substituting (71) into (70), we can finally obtain

$$E[Y_j|W_{i+k}] < E[Y_j|W_{i-1}]. \quad (72)$$

This finishes the proof of Proposition 2.

APPENDIX D PROOF OF LEMMA 1

Calculate the integrals as (73)-(75) on the top of the next page, where (74) follows since $w^* > w > 0$, $g_2(w) - g_1(w) > 0$ in the interval $(0, w^*)$, and $w > w^* > 0$, $g_1(w) - g_2(w) > 0$ in the interval (w^*, ∞) . This finishes the proof of Lemma 1.

Lemma 1 has an intuitive explanation as follows. Two functions having the same integral value mean that the areas under the functions are equal. If the two functions have one and only one cross point at $(w^*, g_i(w^*))$, one of the functions must have larger area on the left side of the cross point, and smaller area on the right side. Then, $w \cdot g_i(w)$ is to scale $g_i(w)$ by w , and the area for $w < w^*$ is enlarged less than the area for $w^* < w$. Consequently, the curve higher than another when $w^* < w$ will have larger area in $[0, \infty)$ after scaled by w . To help better understand this lemma, we call it *integral scaling lemma*.

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$$\int_0^\infty g_2(w)dw = \int_0^\infty g_1(w)dw \quad (73)$$

$$\begin{aligned} \int_0^{w^*} g_2(w)dw + \int_{w^*}^\infty g_2(w)dw &= \int_0^{w^*} g_1(w)dw + \int_{w^*}^\infty g_1(w)dw \\ \int_0^{w^*} g_2(w)dw - \int_0^{w^*} g_1(w)dw &= \int_{w^*}^\infty g_1(w)dw - \int_{w^*}^\infty g_2(w)dw \\ \int_0^{w^*} w^* g_2(w)dw - \int_0^{w^*} w^* g_1(w)dw &= \int_{w^*}^\infty w^* g_1(w)dw - \int_{w^*}^\infty w^* g_2(w)dw \\ \int_0^{w^*} w g_2(w)dw - \int_0^{w^*} w g_1(w)dw &< \int_{w^*}^\infty w g_1(w)dw - \int_{w^*}^\infty w g_2(w)dw \end{aligned} \quad (74)$$

$$\begin{aligned} \int_0^{w^*} w g_2(w)dw + \int_{w^*}^\infty w g_2(w)dw &< \int_0^{w^*} w g_1(w)dw + \int_{w^*}^\infty w g_1(w)dw \\ \int_0^\infty w g_2(w)dw &< \int_0^\infty w g_1(w)dw. \end{aligned} \quad (75)$$

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