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Description	

A Dynamic Attribute-Based Group Signature Scheme and its Application in an Anonymous Survey for the Collection of Attribute Statistics

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Abstract—Recently, cryptographic schemes based on the user’s attributes have been proposed. An Attribute-Based Group Signature (ABGS) scheme is a kind of group signature schemes, where a user with a set of attributes can prove anonymously whether she has these attributes or not. An access tree is applied to express the relationships among some attributes. However, previous schemes do not provide the changing an access tree. In this paper, we propose a Dynamic ABGS scheme that enables an access tree to be changed. Our ABGS is efficient in that re-issuing of the attribute certificate previously issued for each user is not necessary. Moreover, calculations depending on the number of attributes are calculated on the domain of a pairing. Therefore, the number of calculations in a pairing does not depend on the number of attributes associated with a signature. Finally, we discuss how our ABGS can be applied to an anonymous survey for collection of attribute statistics.

Index Terms—Attribute-based system, Group signature, Anonymous Authentication, Anonymous survey

I. INTRODUCTION

Recently, cryptographic schemes based on the user’s attributes have been proposed. Attribute-Based Group Signature (ABGS) schemes [9], [10] are a kind of Group Signature (GS) schemes [7], [11], where a user with a set of attributes can prove anonymously whether she has these attributes or not. ABGS schemes have been proposed by Khader [9], [10] using Goyal’s attribute-based encryption scheme [8] and Boneh’s GS scheme [5]. To the best of our knowledge, these are the only proposals for an ABGS. Usually, users have many kinds of attributes, and there exist some relationships among these attributes. An access tree [8], [9], [10] is applied to express these relationships. However, [9] and [10] schemes do not provide the changing of the relationships among attributes. This means that attributes and relationships among these attributes can be determined only once. This is not practical. Moreover, in all previous ABGSs [9], [10], the number of calculations in a pairing depends on the number of attributes associated with a signature.

Our Contribution : In this paper, we propose a Dynamic ABGS scheme that enables an access tree to be changed. Our ABGS is efficient in that re-issuing of the attribute certificate previously issued for each user is not necessary.

Moreover, calculations depending on the number of attributes are calculated on the domain of a pairing. Therefore, the number of calculations in a pairing does not depend on the number of attributes associated with a signature. Finally, we discuss how our ABGS can be applied to an anonymous survey for collection of attribute statistics.

Organization : The paper is organized as follows. Definitions are given in Section II. Our scheme is described in Section III. Security analysis is performed in Section IV. Efficiency comparisons are presented in Section V. The application of our ABGS in an anonymous survey for the Collection of Attribute Statistics is demonstrated in Section VI.

II. DEFINITIONS

A. Bilinear Groups

Definition 1: (Bilinear Groups) We use bilinear groups and a bilinear map defined as follows:

- 1) \mathbb{G}_1 , \mathbb{G}_2 and \mathbb{G}_3 are cyclic groups of prime order p .
- 2) g_1 and g_2 are generators of \mathbb{G}_1 and \mathbb{G}_2 , respectively.
- 3) ψ is an efficiently computable isomorphism $\psi : \mathbb{G}_2 \rightarrow \mathbb{G}_1$ with $\psi(g_2) = g_1$.
- 4) e is an efficiently computable bilinear map $e : \mathbb{G}_1 \times \mathbb{G}_2 \rightarrow \mathbb{G}_3$ with the following properties.
 - Bilinearity : for all $u, u' \in \mathbb{G}_1$ and $v, v' \in \mathbb{G}_2$, $e(uu', v) = e(u, v)e(u', v)$ and $e(u, vv') = e(u, v)e(u, v')$.
 - Non-degeneracy : $e(g_1, g_2) \neq 1_{\mathbb{G}_3}$ ($1_{\mathbb{G}_3}$ is the \mathbb{G}_3 ’s unit).

B. Access Tree

Let $Att = \{att_1, \dots, att_m\}$ be a set of attributes. For $\Gamma \subseteq 2^{Att} \setminus \{\emptyset\}$, Γ satisfies the monotone property: if $\forall B, C \subseteq Att$, $B \in \Gamma$ and $B \subseteq C$, then $C \in \Gamma$ holds. Let access structures for Att be a set of Γ which satisfies the monotone property. An access tree [8], [9], [10] T is used for expressing an access structure by using a tree structure. An access tree is a tree, where threshold gates are defined on each interior node of the tree, and the leaves are associated with attributes. These attributes are subsets of Att . Let ℓ_x be the number of children of node x , and k_x ($0 < k_x \leq \ell_x$) be the threshold value on the

threshold gate of node x . We call the threshold gate “OR gate” when $k_x = 1$, and “AND gate” when $k_x = \ell_x$. The notation $Leaves \models T$ expresses the fact that a set of attributes $Leaves$ satisfies the access tree T .

C. Model and Security Definitions

In this subsection, we define the model of an ABGS. An ABGS is a kind of GS, where a user U_i with a set of attributes $\Gamma_i \subseteq Att = \{att_1, \dots, att_m\}$ can prove anonymously whether she has these attributes or not. U_i has a membership certificate A_i and a set of attribute certificates $\{T_{i,j}\}_{att_j \in \Gamma_i}$. U_i makes a group signature associated with $\zeta \subseteq \Gamma_i$. Usually, for a set of attributes Att , we construct an access tree to consider all relationships among these attributes. However, the access tree is changed when some threshold values are changed, or some attributes are deleted. Therefore, we define the model of the ABGS accepting a change of an access tree. We do not provide for the fact that a new attribute $att \notin Att = \{att_1, \dots, att_m\}$ is added in an access tree. In this case, we have to re-issue an attribute certificate for users with att to execute the Join algorithm again. Let GM be the group manager. k the security parameter, $params$ the system parameter, $Att = \{att_1, \dots, att_m\}$ the universe of attributes, T_r the r -th access tree with a set of attributes $\{att\}$, where $att \in Att$ is assigned on each leaf, \mathcal{T}_r the public values associated with T_r , gpk the group public key, ik the group secret key which is used for issuing a membership certificate and making \mathcal{T}_r , ok the opening key which is used for the opening procedure to reveal the signers' identification from the group signature, (upk_i, usk_i) the verification/signing key of a signature scheme $DSig$, sk_i the member secret key for U_i ($i = 1, 2, \dots, n$), $\Gamma_i \subseteq Att$ attributes of U_i , and reg be the registration table for Open algorithm. Note that sk_i includes both A_i and $\{T_{i,j}\}_{att_j \in \Gamma_i}$. In Join algorithm, we use the notation $Join(\langle \text{input of } GM \rangle, \langle \text{input of user} \rangle)$.

Definition 2: ABGS

- **Setup**(1^k): This algorithm takes as input k , and returns $params$.
- **KeyGen**($params$): This algorithm takes as input $params$, and returns gpk, ik, ok and $reg = \emptyset$.
- **BuildTree**($params, ik, T_r$): This algorithm takes as input $params, ik$ and T_r whose leaves are associated with a subset of Att , and returns \mathcal{T}_r .
- **Join**($\langle params, gpk, ik, upk_i, \Gamma_i \rangle, \langle params, gpk, upk_i, usk_i \rangle$): This algorithm takes as input $params, gpk, ik, upk_i$ and Γ_i from GM , and $params, gpk, upk_i$ and usk_i from U_i , and returns sk_i and reg .
- **Sign**($param, gpk, sk_i, M, \zeta_i, \mathcal{T}_r$): Let $\zeta_i \subseteq \Gamma_i$ be a set of attributes such that $\zeta_i \models T_r$. This algorithm takes as input $params, gpk, sk_i$, a message M , ζ_i and \mathcal{T}_r , and returns σ associated with ζ_i .
- **Verify**($param, gpk, M, \sigma, \zeta, \mathcal{T}_r$): This algorithm takes as input $params, gpk, \sigma, M, \sigma, \zeta$ and \mathcal{T}_r , and returns 1 if and only if σ is a valid signature.
- **Open**($param, gpk, ok, \sigma, \zeta, \mathcal{T}_r, M, reg$): This algorithm takes as input $params, gpk, ok, \sigma, \zeta, \mathcal{T}_r, M$ and reg ,

and returns the signer's identity i . If the signer is not included in reg , then this algorithm returns 0.

If the access tree T_r is changed to T_{r+1} , then GM runs $BuildTree(params, ik, T_{r+1})$, and opens \mathcal{T}_{r+1} , which is the public information associated with T_{r+1} .

Definition 3: Anonymity : Anonymity requires that for all PPT \mathcal{A} , the advantage of \mathcal{A} on the following game, is negligible.

- **Setup:** Let T_0 be the initial access tree. The challenger runs $KeyGen(params)$, and obtains gpk, ik and ok . Moreover, the challenger runs $BuildTree(params, ik, T_0)$, and obtains \mathcal{T}_0 . \mathcal{A} is given $params, gpk, \mathcal{T}_0$ and ik .
- **Phase1:** \mathcal{A} can send these queries as follows:
 - **Join** : \mathcal{A} requests the join procedure for honest member U_i . \mathcal{A} plays the role of corrupted GM on these queries.
 - **Signing** : \mathcal{A} requests a group signature σ for all messages M , and all members U_i with a set of attributes $\zeta_i \subseteq \Gamma_i$.
 - **Corruption** : \mathcal{A} requests the secret key sk_i for all members U_i .
 - **Open** : \mathcal{A} requests the signer's identity with a message M and a valid signature σ .
 - **Re-BuildTree** : \mathcal{A} sends an access tree T_r . The challenger returns public values \mathcal{T}_r .
- **Challenge:** \mathcal{A} outputs M^* , non-corrupted users U_{i_0}, U_{i_1} and ζ . Note that $\zeta \subseteq \Gamma_{i_0}, \zeta \subseteq \Gamma_{i_1}$ and $\zeta \models T^*$, where T^* is the access tree on the challenge phase. The challenger uniformly selects $b \in_R \{0, 1\}$, and responds with a group signature on M^* by group member U_{i_b} .
- **Phase2:** \mathcal{A} can make the Signing, Corruption, Open, Join and Re-BuildTree queries. Note that Corruption queries include both U_{i_0} and U_{i_1} .
- **Output:** \mathcal{A} outputs a bit b' , and wins if $b' = b$.

The advantage of \mathcal{A} is defined as $Adv^{anon}(\mathcal{A}) = |\Pr(b = b') - \frac{1}{2}|$.

In Join queries, \mathcal{A} can play the role of corrupted GM (the same as in $SndToU$ oracle, which is defined in [2]). Moreover, we consider the Anonymity for Key-Exposure, namely, corruption queries for U_{i_0} and U_{i_1} can be admitted in Phase 2. Even after a secret key is exposed, signatures produced by the member before Key-Exposure remain anonymous. A similar definition of our Key-Exposure has been given in [3] for the ring signature scheme. Moreover, our definition is the CCA-Anonymity model [5], [7], namely, open queries in the Anonymity game can be admitted.

Definition 4: Traceability requires that for all PPT \mathcal{A} , the probability that \mathcal{A} wins the following game is negligible.

- **Setup:** Let T_0 be the initial access tree. The challenger runs $KeyGen(params)$, and obtains gpk, ik and ok . Moreover, the challenger runs $BuildTree(params, ik, T_0)$, and obtains \mathcal{T}_0 . \mathcal{A} is given $params, gpk, \mathcal{T}_0$ and ok .

- **Queries:** \mathcal{A} can issue the Signing, Corruption, Join and Re-BuildTree queries. All queries are the same as in the Anonymity game, except Join.
 - **Join :** \mathcal{A} requests the Join procedure for corrupted member U_i .

- **Output:** \mathcal{A} outputs a message M^* , σ^* and ζ^* . Moreover, T^* is the access tree in this phase, and \mathcal{T}^* is the public information associated with T^* .

\mathcal{A} wins if (1) $\text{Verify}(params, gpk, M^*, \sigma^*, \zeta^*, T^*) = 1$, (2) $\text{Open}(params, gpk, ok, \sigma^*, \zeta^*, T^*, M^*, reg) = 0$, and (3) \mathcal{A} has not obtained σ^* in Signing queries on M^* , ζ^* and T^* . The advantage of \mathcal{A} is defined as the probability of \mathcal{A} wins.

In Join queries, \mathcal{A} can play the role of corrupted users (the same as in SndTol oracle, which is defined in [2]).

Definition 5: Collusion-Resistance requires that for all PPT \mathcal{A} , the probability that \mathcal{A} wins the following game is negligible.

- **Setup:** Let T_0 be the initial access tree. The challenger runs $\text{KeyGen}(params)$, and obtains gpk , ik and ok . Moreover, the challenger runs $\text{BuildTree}(params, ik, T_0)$, and obtains \mathcal{T}_0 . \mathcal{A} is given $params$, gpk and \mathcal{T}_0 .
- **Queries:** \mathcal{A} can issue the Signing, Corruption, Join and Re-BuildTree queries. All queries are the same as in the Anonymity game.
- **Output:** Finally, \mathcal{A} outputs M^* , σ^* and ζ^* . T^* is the access tree in this phase, and \mathcal{T}^* is the public information associated with T^* .

\mathcal{A} wins if (1) $\text{Verify}(params, gpk, M^*, \sigma^*, \zeta^*, T^*) = 1$, and (2) \mathcal{A} has not obtained attribute certificates associated with ζ^* corresponding to a single user.

This property indicates that, for example, there are two users U_{i_0} and U_{i_1} with $\{T_{i_0, j}\}_{att_j \in \Gamma_{i_0}}$ and $\{T_{i_1, j}\}_{att_j \in \Gamma_{i_1}}$, respectively. We assume that $\Gamma_{i_0} \subset \zeta^* \wedge \Gamma_{i_0} \neq \zeta^*$, $\Gamma_{i_1} \subset \zeta^* \wedge \Gamma_{i_1} \neq \zeta^*$, and that $\zeta^* \subseteq \Gamma_{i_0} \cup \Gamma_{i_1}$ hold. Then U_{i_0} and U_{i_1} cannot make a valid group signature with ζ^* even if U_{i_0} and U_{i_1} collude with each other.

Definition 6: Non-Frameability requires that for all PPT \mathcal{A} , the probability that \mathcal{A} wins the following game is negligible.

- **Setup:** Let T_0 be the initial access tree. The challenger runs $\text{KeyGen}(params)$, and obtains gpk , ik and ok . Moreover, the challenger runs $\text{BuildTree}(params, ik, T_0)$, and obtains \mathcal{T}_0 . \mathcal{A} is given $params$, gpk , \mathcal{T}_0 , ik and ok .
- **Queries:** \mathcal{A} can issue the Signing, Corruption, Join and Re-BuildTree queries. All queries are the same as in the Anonymity game.
- **Output:** Finally, \mathcal{A} outputs a message M^* , an honest member U_{i^*} , σ^* and ζ^* . T^* is the access tree in this phase, and \mathcal{T}^* is the public information associated with T^* .

\mathcal{A} wins if (1) $\text{Verify}(params, gpk, M^*, \sigma^*, \zeta^*, T^*) = 1$, (2) σ^* opens to an honest member U_{i^*} , (3) \mathcal{A} has not obtained σ^* in Signing queries on M^* , U_{i^*} and ζ^* , and (4) \mathcal{A} has not

obtained sk_{i^*} in Corruption queries on U_{i^*} . The advantage of \mathcal{A} is defined as the probability of \mathcal{A} wins.

III. PROPOSED SCHEMES

In this section, an ABGS together with an assignment of secret values to access trees is presented.

A. Assignment of Secret Values to Access Trees

The previous schemes [10], [9] use a ‘‘Top-Down Approach’’ construction for access trees (when threshold gates are defined on each interior node of the tree and the leaves are associated with attributes) as follows:

- A secret value of the root node is chosen.
- A polynomial $q_{root}(x)$ of degree ‘‘threshold value -1 ’’ is defined such that $q_{root}(0)$ equals the secret value of the root node.
- A secret value of a child node is defined such as $q_{root}(index(child))$.
- Secret values of all nodes can be defined to execute this procedure recursively.

If the access tree is changed, then the above Top-Down Approach construction has to be executed again. This means that the secret values that are associated with attributes have to be re-issued to corresponding users, because these values have to be changed. In our proposal, a ‘‘Bottom-Up Approach’’ construction is introduced. The order of our construction is *different from that of* the Top-Down Approach construction, namely, first all secret values are chosen for each attribute associated with each leaf. These secret values of leaves will not be changed when the access tree is changed.

Idea : For a node x associated with the threshold value k_x , $\ell_x - k_x$ dummy nodes will be opened, where ℓ_x is the number of children of x . Next, the threshold value is changed from k_x to ℓ_x . Then, all threshold gates become AND gates. Children with k_x or more can compute the secret value of their parent node by using the number of $\ell_x - k_x$ public dummy nodes. We define functions **AddDummyNode** which adds dummy nodes to the access tree, **AssignedValue** which assigns secret values for nodes on the access tree, and **MakeSimplifiedTree** which makes a simplified tree associated with a set of leaves. Let $index$ be the function which returns the index of the node, and p be a prime number. We assume that T includes Att .

$\langle \text{AddDummyNode}(T) \rangle$: This algorithm takes as input T , and returns the extended access tree T^{ext} .

- 1) For an interior node x of T , the number of dummy nodes $\ell_x - k_x$ is added to x ’s children.
- 2) The threshold value defined in x is changed from k_x to ℓ_x .
- 3) All nodes are assigned unique index numbers.
- 4) The resulting tree, called T^{ext} , is outputted.

Let D_T be a set of dummy nodes determined by **AddDummyNode**. We assume that T^{ext} includes D_T . Moreover, let $s_j \in \mathbb{Z}_p$ be a secret value for an attribute $att_j \in Att$. Let $S = \{s_j\}_{att_j \in Att}$.

$\langle \text{AssignedValue}(p, S, T^{ext}) \rangle$: This algorithm takes as input p , S and T^{ext} and returns a secret value $s_x \in \mathbb{Z}_p$ for each node

x of T^{ext} . Let $\{child\}_x$ be the set of node x 's children except the dummy nodes, and $\{d\}_x$ be the set of node x 's dummy nodes.

- 1) For an interior node x of T^{ext} , a polynomial q_x of degree $\ell_x - 1$ is assigned as follows:
 - a) For $att_j \in \{child\}_x$, let q_x be a polynomial of degree at most $\ell_x - 1$ which passes through $(index(att_j), s_j)$, where $s_j \in S$ ($j = 1, 2, \dots, \ell_x$).
 - b) For a dummy node $d_j \in \{d\}_x$, the secret value $s_{d_j} := q_x(index(d_j))$ ($j = 1, 2, \dots, \ell_x - k_x$) is assigned.
 - c) For x , $s_x := q_x(0)$ is assigned.
- 2) Repeat the above procedure up to the root node, $s_T := q_{root}(0)$ is the secret value of T .
- 3) Output $\{s_{d_j}\}_{d_j \in D_T}$ and s_T .

$\langle \text{MakeSimplifiedTree}(Leaves, T^{ext}) \rangle$: This algorithm takes as input the set of attributes $Leaves \subseteq Att$ satisfying $Leaves \models T$, and returns the simplified access tree T^{Leaves} (which is the access tree associated with $Leaves$) and a product of Lagrange coefficients Δ_{leaf} .

- 1) The set of attributes $\{att_j\}_{att_j \in Att \setminus Leaves}$ are deleted from T^{ext} .
- 2) An interior node x has children less than the threshold value (namely, ℓ_x), and is deleted from T^{ext} along with x 's descendants.
- 3) Let D^{Leaves} be the set of dummy nodes which have remained after (1) and (2), and T^{Leaves} be the access tree after (1) and (2).
- 4) For all nodes x of T^{Leaves} except root, we define L_x as follows:
 - a) For x , define the depth 2 subtree of T^{Leaves} with x as leaf node. Let c_x be the set of indices of leaves.
 - b) Compute $L_x := \prod_{k \in c_x} \frac{-k}{index(x) - k}$.
- 5) Let $leaf \in \{att_j \in Leaves\} \cup \{d_j \in D^{Leaves}\}$ be a leaf node of T^{Leaves} . For $leaf$, we define Δ_{leaf} as follows:
 - a) Let $Path_{leaf} := \{leaf, parent_1, \dots, parent_{n_{leaf}} = root\}$ be the set of nodes that appears in the path from $leaf$ to root node.
 - b) Compute $\Delta_{leaf} := \prod_{node \in Path_{leaf} \setminus root} L_{node}$.
- 6) Output T^{Leaves} , Δ_j ($att_j \in Leaves$), Δ_{d_j} ($d_j \in D^{Leaves}$).

Clearly, $\sum_{att_j \in Leaves} \Delta_j s_j + \sum_{d_j \in D^{Leaves}} \Delta_{d_j} s_{d_j} = s_T$ holds.

B. Proposed Attribute-Based Group Signature Scheme

In this subsection, we propose the ABGS by using our assignment (Section III-A). Our ABGS uses the Cramer-Shoup encryption scheme [6] for both CCA-Anonymity and Key-Exposure properties, and a concurrently secure Join algorithm proposed in [7]. Let $NIZK$ be a Non-Interactive Zero-Knowledge proof, SPK be a Signature of Proof of Knowledge, and $Ext-Commit$ be an extractable

commitment scheme. Let T_0 be the initial access tree. Note that if an access tree is changed, then GM runs $\text{BuildTree}(params, ik, T_{r+1})$, and opens T_{r+1} , which is the public information associated with T_{r+1} .

- **Setup(1^k)**
 - 1) GM selects cyclic groups of $\mathbb{G}_1, \mathbb{G}_2$, and \mathbb{G}_3 with prime order p , an isomorphism $\psi : \mathbb{G}_2 \rightarrow \mathbb{G}_1$, a bilinear map $e : \mathbb{G}_1 \times \mathbb{G}_2 \rightarrow \mathbb{G}_3$, and a hash function $\mathcal{H} : \{0, 1\}^* \rightarrow \mathbb{Z}_p$.
 - 2) GM selects a generator $g_2 \in \mathbb{G}_2$ and $g_3, g_4 \in_R \mathbb{G}_1$, and sets $g_1 = \psi(g_2)$.
 - 3) GM defines $Att = \{att_1, att_2, \dots, att_m\}$.
 - 4) GM outputs $params = (\mathbb{G}_1, \mathbb{G}_2, \mathbb{G}_3, e, \psi, \mathcal{H}, g_1, g_2, g_3, g_4, Att)$.
- **KeyGen($params$)**
 - 1) GM selects $\gamma \in_R \mathbb{Z}_p$, and computes $\omega = g_2^\gamma$.
 - 2) GM selects $x'_1, x'_2, y'_1, y'_2, z \in_R \mathbb{Z}_p$, and computes $C = g_3^{x'_1} g_4^{x'_2}, D = g_3^{y'_1} g_4^{y'_2}$ and $E = g_3^z$.
 - 3) For $att_j \in Att$, GM selects $s_j \in_R \mathbb{Z}_p^*$, sets $S = \{s_j\}_{att_j \in Att}$, and computes $g_{att_j} = g_2^{s_j}$ ($att_j \in Att$).
 - 4) For $att_j \in Att$, GM selects $h_j \in_R \mathbb{G}_2$, and sets $\hat{h}_j = \psi(h_j)$.
 - 5) GM outputs $ok = (z), gpk = (\omega, C, D, E, \{h_j\}_{j=1}^m, \{g_{att_j}\}_{att_j \in Att})$ and $ik = (\gamma, \{s_j\}_{att_j \in Att})$.
- **BuildTree($params, ik, T_0$)**
 - 1) GM runs $T_0^{ext} = \text{AddDummyNode}(T_0)$ and $\text{AssignedValue}(p, S, T_0^{ext})$, and gets $\{s_{d_j}\}_{d_j \in D_{T_0}}$ and s_{T_0} .
 - 2) GM computes $g_{d_j} = g_2^{s_{d_j}}$ ($d_j \in D_{T_0}$) and $v_0 = g_2^{s_{T_0}}$.
 - 3) GM outputs $\mathcal{T}_0 = (\{g_{d_j}\}_{d_j \in D_{T_0}}, v_0, T_0^{ext})$.
- **Join($\langle params, gpk, ik, upk_i, \Gamma_i \rangle, \langle params, gpk, upk_i, usk_i \rangle$)**

U_i gets $sk_i = ((A_i, x_i, y_i), \{T_{i,j}\}_{att_j \in \Gamma_i})$, where (A_i, x_i, y_i) is a member certificate and $\{T_{i,j}\}_{att_j \in \Gamma_i}$ is the set of attribute certificates as follows:

 - 1) U_i picks $y_i \in_R \mathbb{Z}_p$, and computes $c_i = \text{Ext-Commit}(y_i)$, $F_i = E^{y_i}$ and $\pi_1 = \text{NIZK}\{y_i : F_i = E^{y_i} \wedge c_i = \text{Ext-Commit}(y_i)\}$.
 - 2) U_i sends F_i, c_i and π_1 to GM .
 - 3) GM checks π_1 . If π_1 is not valid, then abort.
 - 4) GM selects $x_i \in_R \mathbb{Z}_p$, and computes $A_i = (g_1 F_i)^{1/(\gamma+x_i)}$, $B_i = e(g_1 F_i, g_2)/e(A_i, w)$, $D_i = e(A_i, g_2)$, $T_{i,j} = A_i^{s_j}$ ($att_j \in \Gamma_i$) and $\pi_2 = \text{NIZK}\{x_i, s_j$ ($att_j \in \Gamma_i$) : $B_i = D_i^{x_i} \wedge T_{i,j} = A_i^{s_j}$ ($att_j \in \Gamma_i$) $\wedge g_{att_j} = g_2^{s_j}$ ($att_j \in \Gamma_i$)\}.
 - 5) GM sends $A_i, B_i, D_i, \{T_{i,j}\}_{att_j \in \Gamma_i}$ and π_2 to U_i .
 - 6) U_i checks π_2 . If π_2 is not valid, then abort.
 - 7) U_i makes $S_{i,A_i} = \text{DSig}_{usk_i}(A_i)$, and sends S_{i,A_i} to GM .
 - 8) GM verifies S_{i,A_i} with respect to upk_i and A_i . If S_{i,A_i} is valid, then GM sends x_i to U_i , and adds (U_i, A_i) to reg .

- 9) U_i checks the relation $A_i^{(x_i+\tau)} = g_1 E^{y_i}$ to verify whether $e(A_i, g_2)^{x_i} e(A_i, w) e(E, g_2)^{-y_i} \stackrel{?}{=} e(g_1, g_2)$.

- **Sign**($param, gpk, sk_i, M, \zeta_i, T_r$)

A signer U_i signs a message $M \in \{0, 1\}^*$ as follows:

- 1) U_i chooses $\zeta_i \subseteq \Gamma_i$ ($\zeta_i \models T_r$) to associate ζ_i with a group signature. Let $|\zeta_i| = \phi$.
- 2) U_i runs **MakeSimplifiedTree**(ζ_i, T_r^{ext}), and gets $T_r^{\zeta_i}$, Δ_j ($att_j \in \zeta_i$) and Δ_{d_j} ($d_j \in D_r^{\zeta_i}$).
- 3) U_i computes $g_d = \prod_{d_j \in D_r^{\zeta_i}} g_{d_j}^{\Delta_{d_j}}$.
- 4) U_i selects $\alpha, \delta \in_R \mathbb{Z}_p$, and computes $C_1 = A_i E^\alpha$, $C_2 = g_3^\alpha$, $C_3 = g_4^\alpha$ and $C_4 = (CD^\beta)^\alpha$, where $\beta = \mathcal{H}(C_1, C_2, C_3)$.
- 5) U_i computes $CT_j = T_{i,j} \hat{h}_j^\delta$ ($att_j \in \zeta_i$).
- 6) U_i sets $\tau = \alpha x_i + y_i$, and computes $V = SPK\{(\alpha, x_i, \tau, \delta) : \frac{e(C_1, \omega)}{e(g_1, g_2)} = \frac{e(E, g_2)^{\tau} \cdot e(E, \omega)^{\alpha}}{e(C_1, g_2)^{x_i}} \wedge C_2 = g_3^\alpha \wedge C_3 = g_4^\alpha \wedge C_4 = (CD^\beta)^\alpha \wedge \frac{e(\prod_{att_j \in \zeta_i} CT_j^{\Delta_j}, g_2)}{e(C_1, v_r/g_d)} = \frac{e(\prod_{att_j \in \zeta_i} \hat{h}_j^{\Delta_j}, g_2)^\delta}{e(E, v_r/g_d)^\alpha}\}(M)$.

Concretely, U_i computes V as follows:

- a) U_i selects $r_\alpha, r_{x_i}, r_\tau, r_\delta \in_R \mathbb{Z}_p$.
 - b) U_i computes $R_1 = \frac{e(E, g_2)^{r_\tau} e(E, \omega)^{r_\alpha}}{e(C_1, g_2)^{r_{x_i}}}$, $R_2 = g_3^{r_\alpha}$, $R_3 = g_4^{r_\alpha}$, $R_4 = (CD^\beta)^{r_\alpha}$ and $R_{Att} = \frac{e(\prod_{att_j \in \zeta_i} \hat{h}_j^{\Delta_j}, g_2)^{r_\delta}}{e(E, v_r/g_d)^{r_\alpha}}$.
 - c) U_i computes $c = \mathcal{H}(gpk, M, \{C_i\}_{i=1}^4, \{CT_i\}_{i=1}^\phi, \{R_i\}_{i=1}^4, R_{Att})$.
 - d) U_i computes $s_\alpha = r_\alpha + c\alpha$, $s_{x_i} = r_{x_i} + cx_i$, $s_\tau = r_\tau + c\tau$ and $s_\delta = r_\delta + c\delta$.
- 7) U_i outputs $\sigma = (\{C_i\}_{i=1}^4, c, s_\alpha, s_{x_i}, s_\tau, s_\delta, \{CT_i\}_{i=1}^\phi)$

A signer U_i proves the knowledge of $(\alpha, x_i, \tau, \delta)$ which satisfies the 5 above relations described in SPK V . The first relation captures whether a signer has a valid membership certificate issued by the Join algorithm or not. The last relation captures whether a signer has valid attribute certificates associated with the set of attributes $\zeta_i \models T_r$ or not.

- **Verify**($param, gpk, M, \sigma, \zeta, T_r$)

A verifier verifies a group signature σ associated with the set of attributes ζ .

- 1) The verifier runs **MakeSimplifiedTree**(ζ, T_r^{ext}), and gets T_r^ζ , Δ_j ($att_j \in \zeta$) and Δ_{d_j} ($d_j \in D_r^\zeta$). Let $|\zeta| = \phi$.
- 2) The verifier computes $g_d = \prod_{d_j \in D_r^\zeta} g_{d_j}^{\Delta_{d_j}}$ and $\beta = \mathcal{H}(C_1, C_2, C_3)$.
- 3) The verifier computes $\tilde{R}_1 = \frac{e(E, g_2)^{s_\tau} \cdot e(E, \omega)^{s_\alpha}}{e(C_1, g_2)^{s_{x_i}}}$, $\tilde{R}_2 = \left(\frac{1}{C_2}\right)^c$, $\tilde{R}_3 = g_4^{s_\alpha} \left(\frac{1}{C_3}\right)^c$, $\tilde{R}_4 = (CD^\beta)^{s_\alpha} \left(\frac{1}{C_4}\right)^c$ and $\tilde{R}_{Att} =$

$$\frac{e(\prod_{att_j \in \zeta_i} \hat{h}_j^{\Delta_j}, g_2)^{s_\delta}}{e(E, v_r/g_d)^{s_\alpha}} \left(\frac{e(C_1, v_r/g_d)}{e(\prod_{att_j \in \zeta_i} CT_j^{\Delta_j}, g_2)} \right)^c$$

- 4) The verifier checks $c \stackrel{?}{=} \mathcal{H}(gpk, M, gpk, M, \{C_i\}_{i=1}^4, \{CT_i\}_{i=1}^\phi, \{\tilde{R}_i\}_{i=1}^4, \tilde{R}_{Att})$.

- **Open**($param, gpk, ok, \sigma, \zeta, T_r, M, reg$)

- 1) GM verifies the validity of σ by using **Verify**($param, gpk, M, \sigma, \zeta, T_r$). If σ is not a valid signature, then GM outputs \perp .
- 2) GM computes $A_i = C_1/C_2^z$.
- 3) GM searches A_i from reg , and outputs identity i . If there is no entry in reg , then GM outputs 0.

IV. SECURITY

Let p , q_H and q_S be order of bilinear groups, and the number of hash queries and signature queries, respectively. Our scheme is based on the discrete logarithm (DL), eXternal Diffie-Hellman (XDH) [5] (it is the Decision Diffie-Hellman (DDH) assumption over \mathbb{G}_1), and q -strong Diffie-Hellman (q -SDH) [4] assumptions.

Theorem 1: The proposed scheme satisfies Anonymity under the XDH assumption (namely DDH assumption over \mathbb{G}_1), i.e., $Adv^{anon}(\mathcal{A}) \leq \frac{q_S q_H}{p} + m \cdot \epsilon_{\text{ddh}}$ holds, where ϵ_{ddh} is the DDH-advantage of some algorithms and $m = |Att|$.

Theorem 2: We suppose an adversary \mathcal{A} breaks the Traceability of the proposed scheme with the advantage ϵ . Then, we can construct an algorithm \mathcal{B} that breaks the q -SDH assumption with the advantage $\frac{1}{6} \left(1 - \frac{1}{p}\right) \left(1 - \frac{q_S q_H}{p}\right) \epsilon$.

Theorem 3: We suppose an adversary \mathcal{A} breaks the Non-Frameability of the proposed scheme with the advantage ϵ . Then, we can construct an algorithm \mathcal{B} that breaks the DL assumption with the advantage $\frac{1}{12} \left(1 + \frac{1}{n}\right) \left(1 - \frac{q_S q_H}{p}\right) \epsilon$.

Theorem 4: The probability that a signature by forged attribute certificates passes the verification, $\Pr(\text{Verify}(param, s, gpk, M, \sigma, \zeta, T) = 1 \wedge \zeta \not\models T)$, is $\frac{p^{\phi-1}-1}{p^\phi} = \frac{1}{p} \left(1 - \frac{1}{p^{\phi-1}}\right)$, where ϕ is the number of attributes associated with a signature.

Theorem 5: Even if some malicious participants U_{i_1}, \dots, U_{i_k} ($k > 1$) with the set of attributes $\zeta_{i_1}, \dots, \zeta_{i_k}$ collude, they cannot make a valid signature associated with an attribute tree T_r , where $(\cup_{j=1}^k \zeta_{i_j}) \models T_r$ and $\zeta_{i_j} \not\models T_r$ ($j = 1, \dots, k$) with non-negligible probability.

We omit these proofs, and put them in the full version of this paper.

V. COMPARISONS

Let ζ ($|\zeta| = \phi$) be the set of attributes which is associated with a signature, D_ζ be the set of dummy nodes which is defined as ζ , and $|Att| = m$. Moreover, let r be the number of revoked members [9]. We assume that the computational estimations are made according to [11]. In our scheme, Verification costs are the lowest, because the number of calculations in a pairing does not depend on the number of attributes associated with a signature. There is room for argument regarding the Signing costs. Moreover, our scheme provides Dynamic property,

Table 1. Comparisons

	[10]	[9]	Our Scheme
Dynamic property	no	no	yes
CCA-Anonymity	no	no	yes
Non-Frameability	no	no	yes
Key-Exposure	no	no	yes
Signature Length	$1633 + 171\phi$	$1192 + 1191\phi$	$1634 + 171\phi$
Signing	$(12 + 2\phi)\mathbb{G}_1 + 5\mathbb{G}_3 + e$	$(7 + 2\phi)\mathbb{G}_1 + (5 + \phi)\mathbb{G}_3 + (\phi + 1)e$	$(9 + 3\phi)\mathbb{G}_1 + (\phi + 1)\mathbb{G}_2 + 8\mathbb{G}_3 + 3e$
Verification	$12\mathbb{G}_1 + (\phi + 8)\mathbb{G}_3 + (\phi + 1)e$	$(6 + 2r)\mathbb{G}_1 + (8 + 2\phi)\mathbb{G}_3 + (\phi + 2r + 1)e$	$(11 + 2\phi)\mathbb{G}_1 + (\phi + 1)\mathbb{G}_2 + 14\mathbb{G}_3 + 6e$

VI. APPLICATION OF ABGS IN ANONYMOUS SURVEY FOR COLLECTION OF ATTRIBUTE STATISTICS

In this section, we discuss how our ABGS can be applied to an anonymous survey for collection of attribute statistics. An anonymous survey is used as follows: When we apply the GS to a business system offering some services to group members, each member’s personal information is not exposed. Moreover, a service provider can verify whether each user is valid or not. However, it is difficult for a service provider to obtain a collection of user’s attribute statistics to improve service contents. In [13], an anonymous survey has been proposed which is a protocol executed among trusted third parties (TTPs). Moreover, the relationships among some attributes, e.g., (female \wedge 20s), can be handled in the statistics information. However, a distributor cannot verify whether users properly construct the ciphertext or not. In [12], an anonymous survey has been proposed using the Open algorithm of Ateniese et. al. GS [1]. A distributor can verify whether users properly make the ciphertext or not, to verify the validity of group signatures. Because one attribute certificate is issued for an attribute type, it is difficult as the relationships among some attributes to be handled in the statistics information. There is an obvious solution: new attribute types such as $att_C = att_A \wedge att_B$ are defined. However, the number of all attribute types are represented by $O(2^m)$, where m is the number of all attributes. We solve this attribute increase problem to apply an ABGS.

- 1) A user makes a group signature σ associated with the set of attributes ζ to use our ABGS.
- 2) The user encrypts ζ to use the public key of a distributor, and sends both σ and the encrypted ζ to the distributor.
- 3) The distributor decrypts ζ , and verifies whether σ is valid or not.
- 4) The statistics information is the collection of ζ .

To collect the set of attributes ζ , the distributor can obtain the statistics of attributes without any other information, because the distributor does not know the opening key which is used for the opening procedure to reveal the signer’s identification from the group signature. Moreover, the distributor can verify whether users properly made the ciphertext or not, to verify that the validity of group signatures is the same as in [12]. Moreover, the relationships among some attributes can be handled in the statistics information in the same way as in [13], without increasing the number of attribute certificates of each user. Indeed, the number of attribute certificates of each user is represented by $O(m)$. Of course, relationships

among some attributes which one wants to reflect with the statistics information are different in each case. Our scheme is suitable for use in the anonymous survey because the change of relationships is indispensable in the anonymous survey for the collection of attribute statistics.

VII. CONCLUSION

In this paper, we propose a Dynamic ABGS scheme that enables an access tree to be changed. Our ABGS is efficient in that re-issuing of the attribute certificate previously issued for each user is not necessary. Moreover, the number of calculations in a pairing does not depend on the number of attributes associated with a signature. A service provider obtains a collection of anonymous user’s attribute statistics to improve service contents by using our ABGS.

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